

Deep Learning for Data Science

DS 542

<https://dl4ds.github.io/fa2025/>

Residual Networks



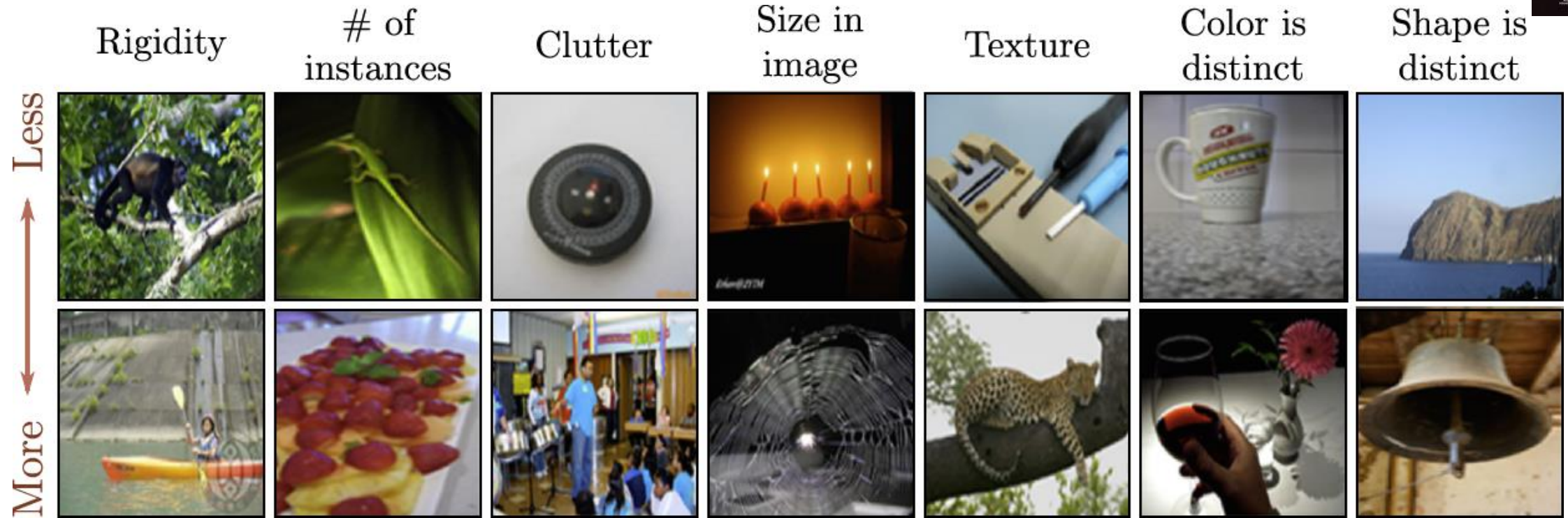
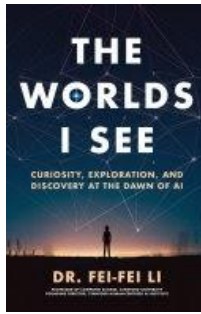
Plan for Today

- Finish up CNN examples (from last time)
- Residual networks
- Image classification
- Object detection
- Semantic segmentation

Project 1:

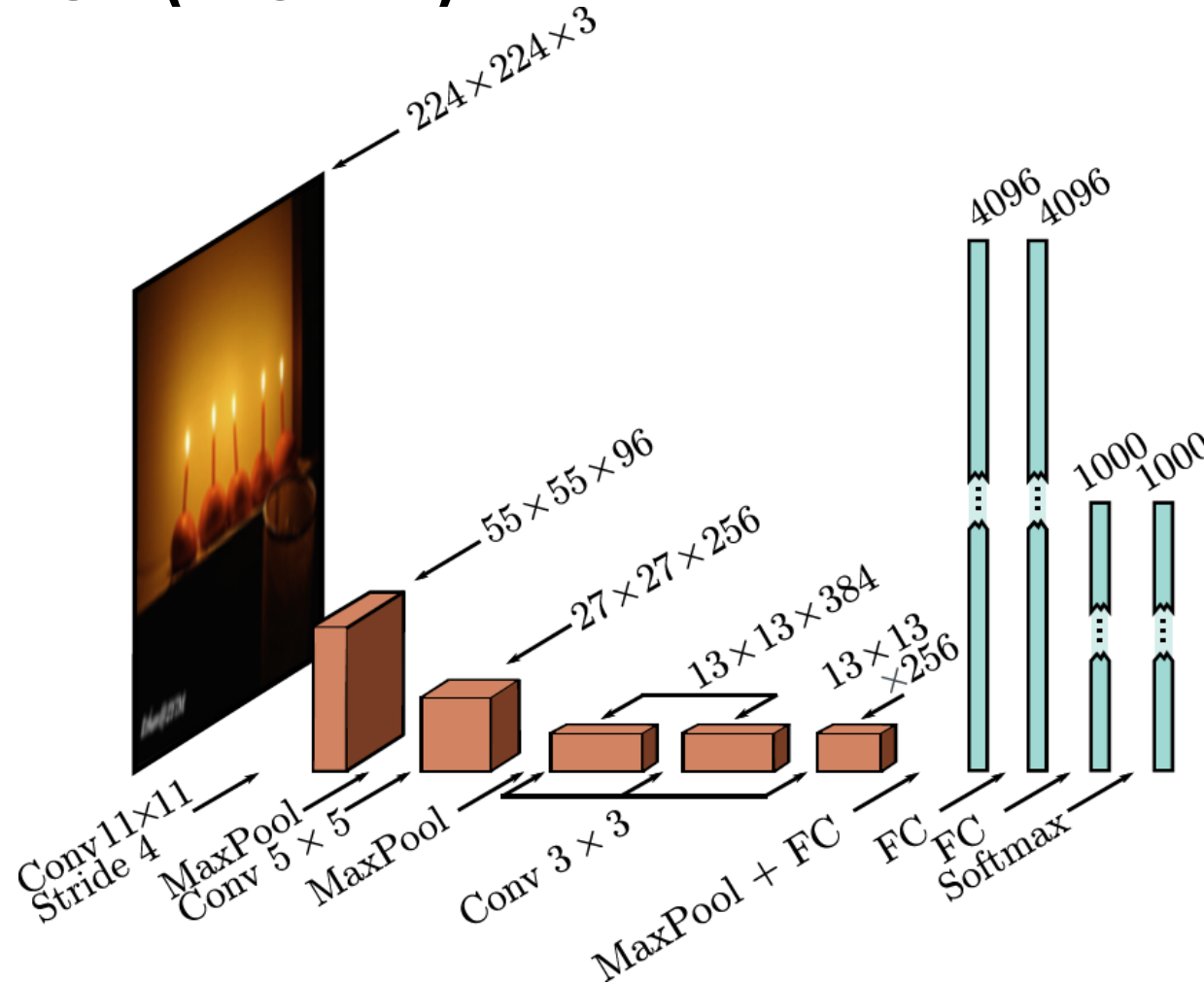
ImageNet 1K database

Fei-Fei Li



- 224 x 224 images
- 1,281,167 training images, 50,000 validation images, and 100,000 test images
- 1000 classes

AlexNet (2012)



Almost all the 60 million parameters are in fully connected layers

A. Krizhevsky, I. Sutskever, and G. E. Hinton, “ImageNet classification with deep convolutional neural networks,” *Commun. ACM*, vol. 60, no. 6, pp. 84–90, May 2012, doi: [10.1145/3065386](https://doi.org/10.1145/3065386).

AlexNet (2012)

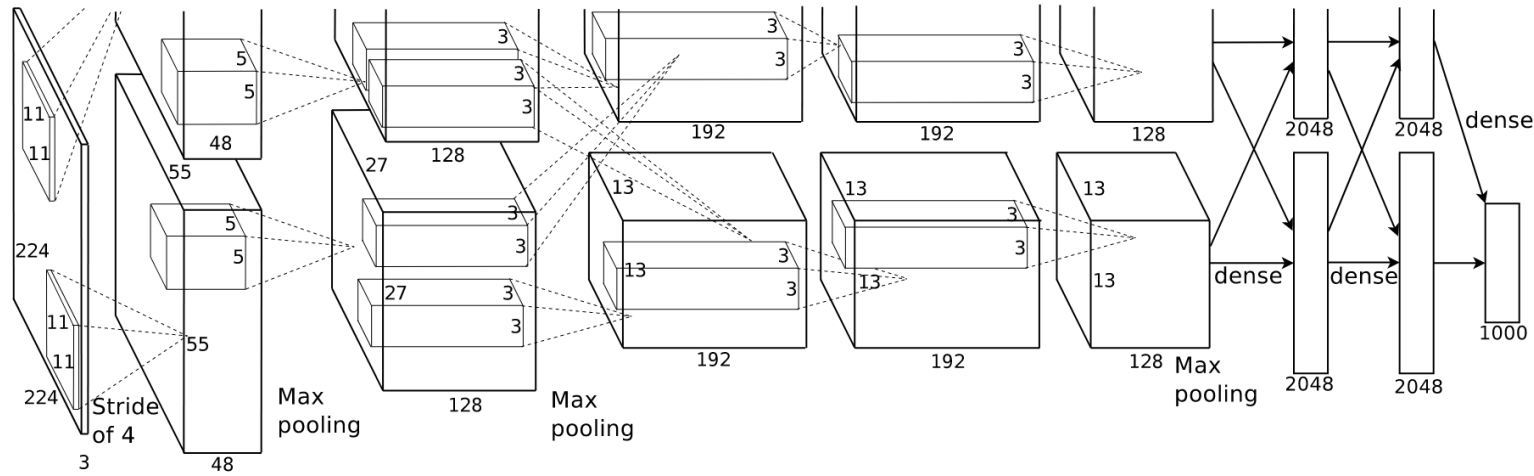


Figure 2: An illustration of the architecture of our CNN, explicitly showing the delineation of responsibilities between the two GPUs. One GPU runs the layer-parts at the top of the figure while the other runs the layer-parts at the bottom. The GPUs communicate only at certain layers. The network's input is 150,528-dimensional, and the number of neurons in the network's remaining layers is given by 253,440–186,624–64,896–64,896–43,264–4096–4096–1000.

Won the 2012 Large-Scale Vision Recognition Challenge (ILSVRC) by a big margin.

Took between five and six days to train on two GTX 580 3GB GPUs with manually optimized compute kernels.

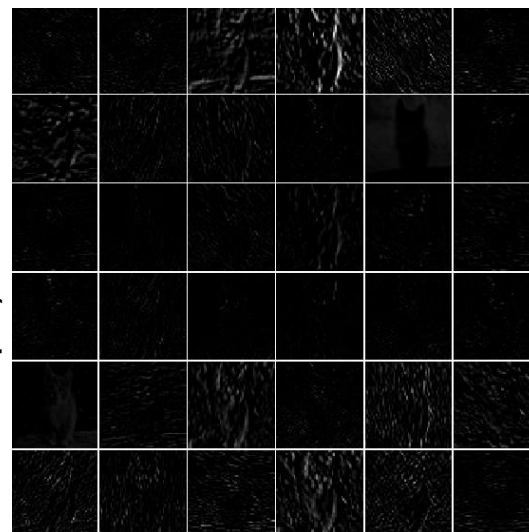
A. Krizhevsky, I. Sutskever, and G. E. Hinton, "ImageNet classification with deep convolutional neural networks," *Commun. ACM*, vol. 60, no. 6, pp. 84–90, May 2012, doi: [10.1145/3065386](https://doi.org/10.1145/3065386).

AlexNet



Cat image input
(not actual image)

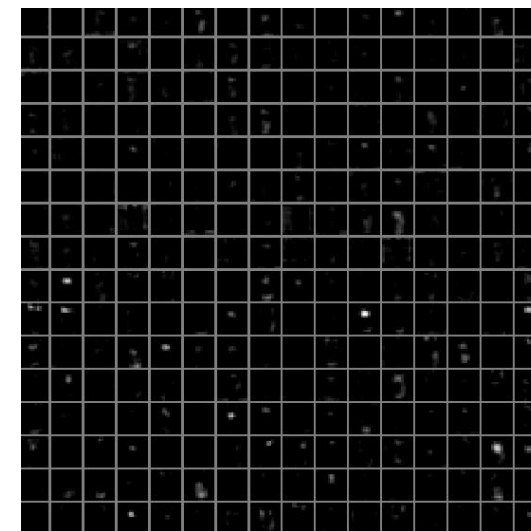
Activations
(feature
maps)



1st Layer

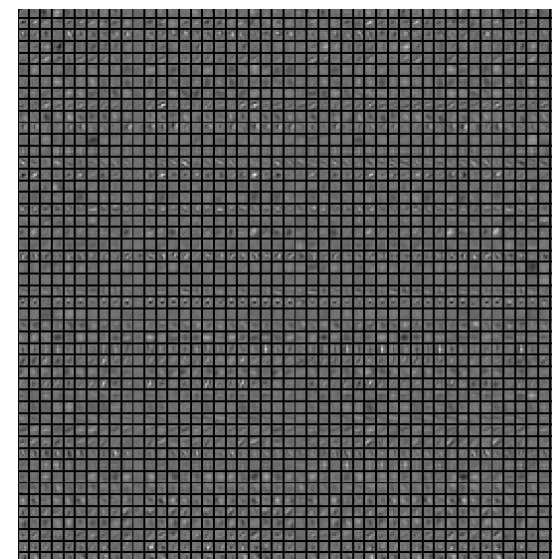
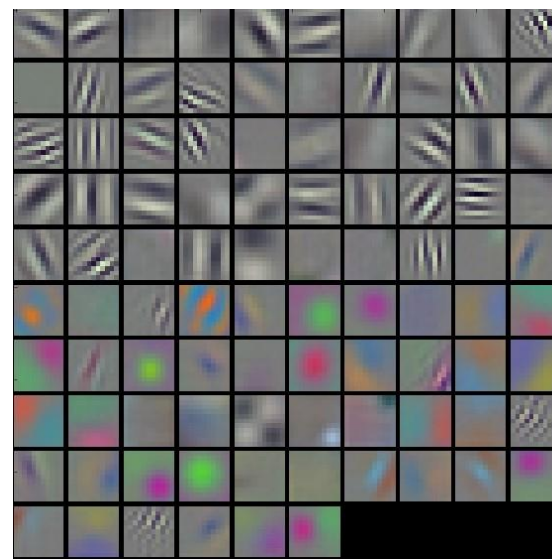
...

2nd Layer



5th Layer

Filter
Kernels

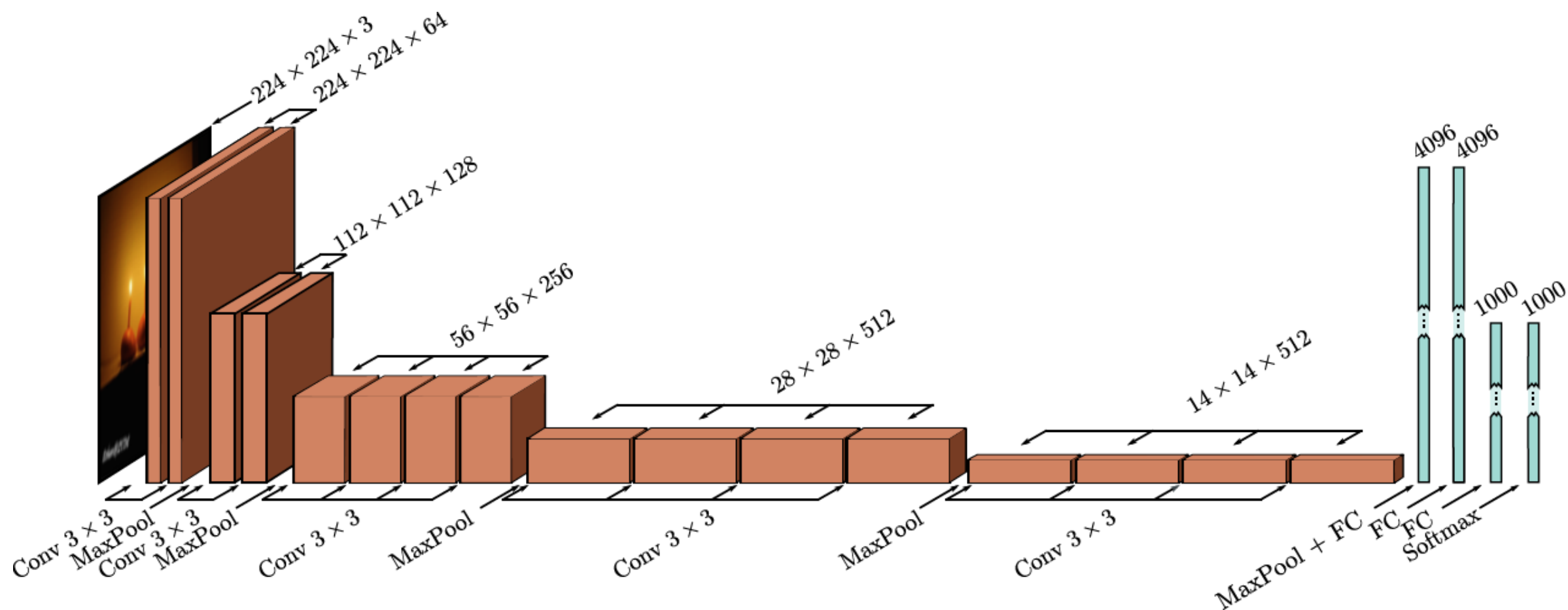


...

Details

- At test time average results from five different cropped and mirrored versions of the image
- SGD with a momentum coefficient of 0.9 and batch size of 128.
- L2 (weight decay) regularizer used.
- This system achieved a 16.4% top-5 error rate and a 38.1% top-1 error rate.

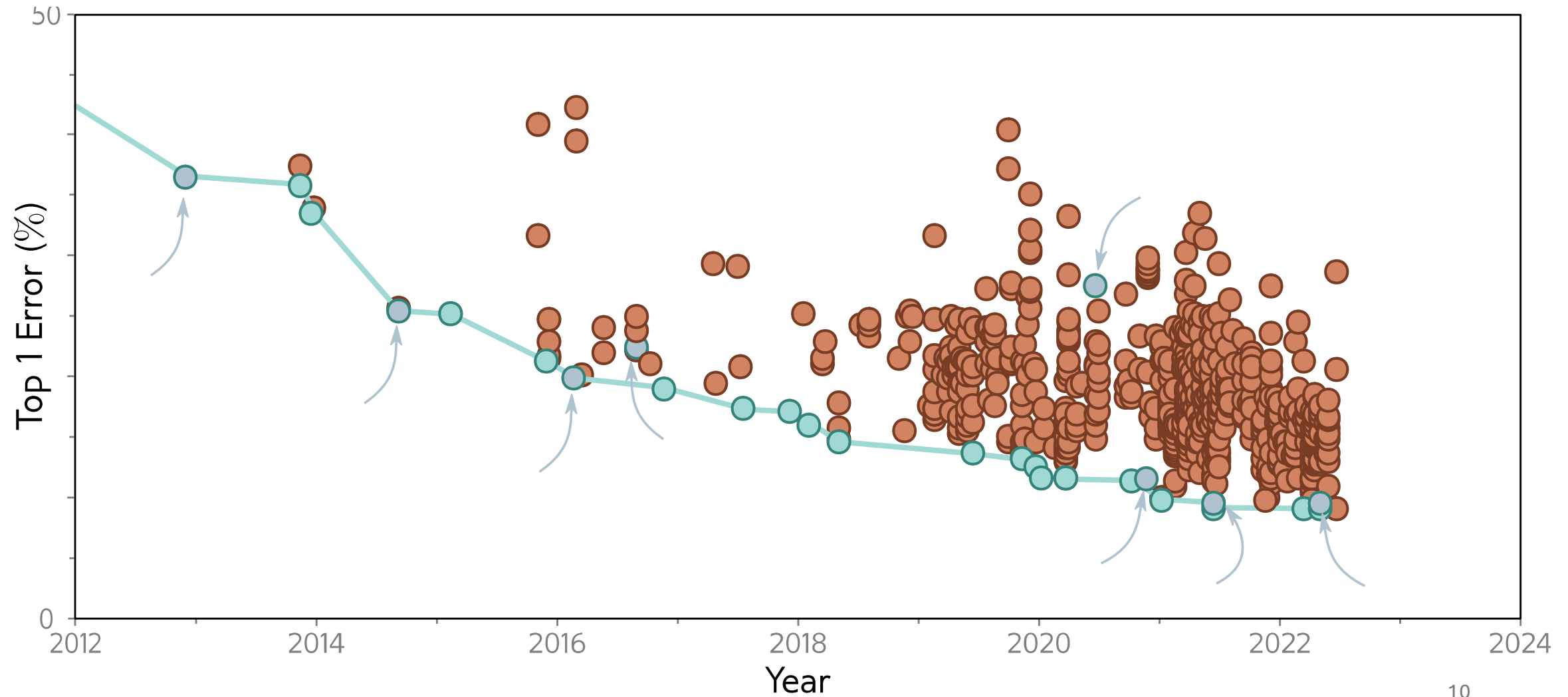
VGG (2015)



Details

- 19 hidden layers
- 144 million parameters
- 6.8% top-5 error rate, 23.7% top-1 error rate

ImageNet History



Any Questions?

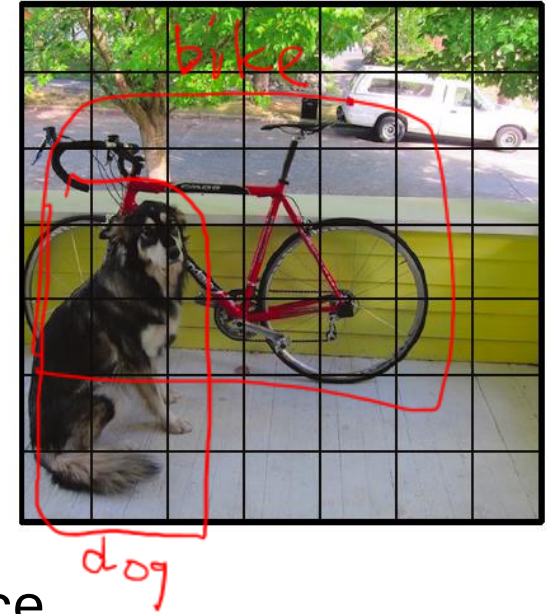
???

Moving on

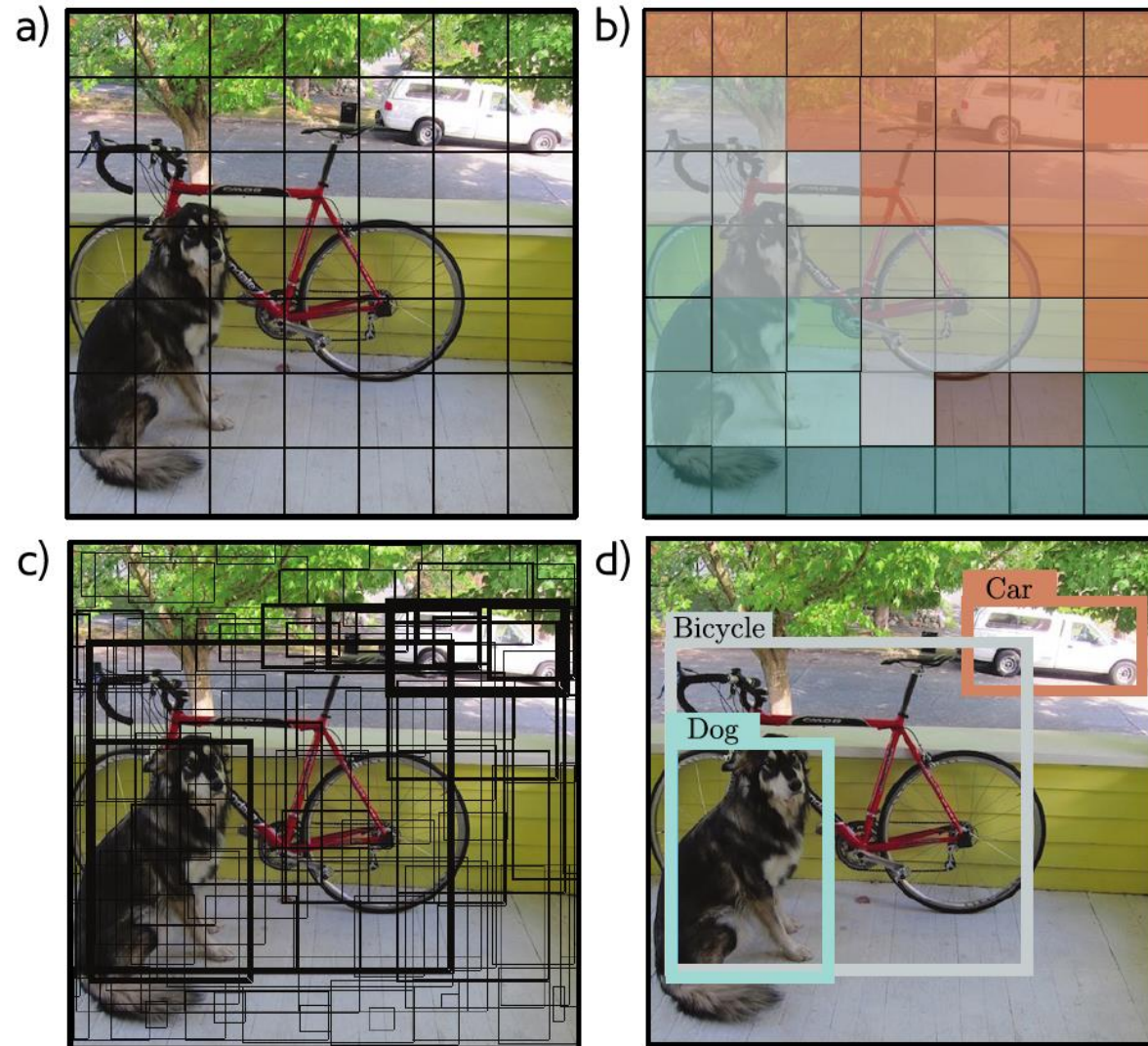
- Image classification
- Object detection
- Semantic segmentation

You Only Look Once (YOLO)

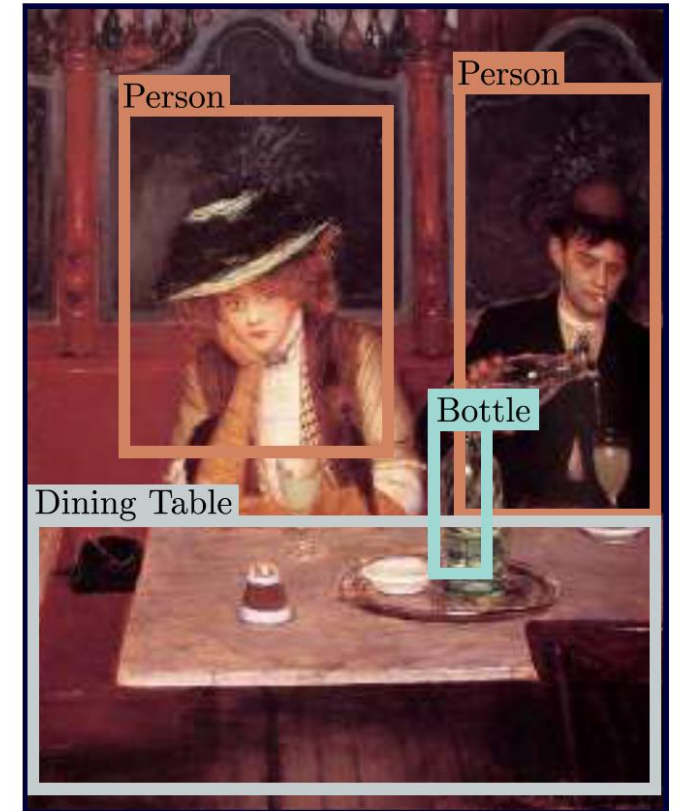
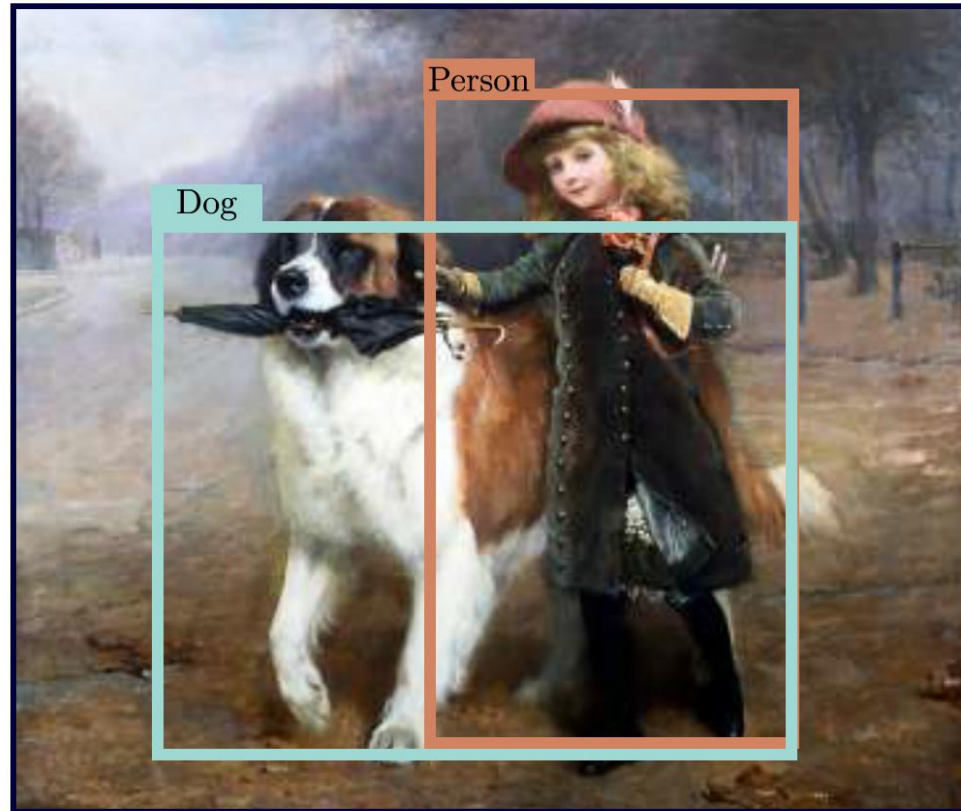
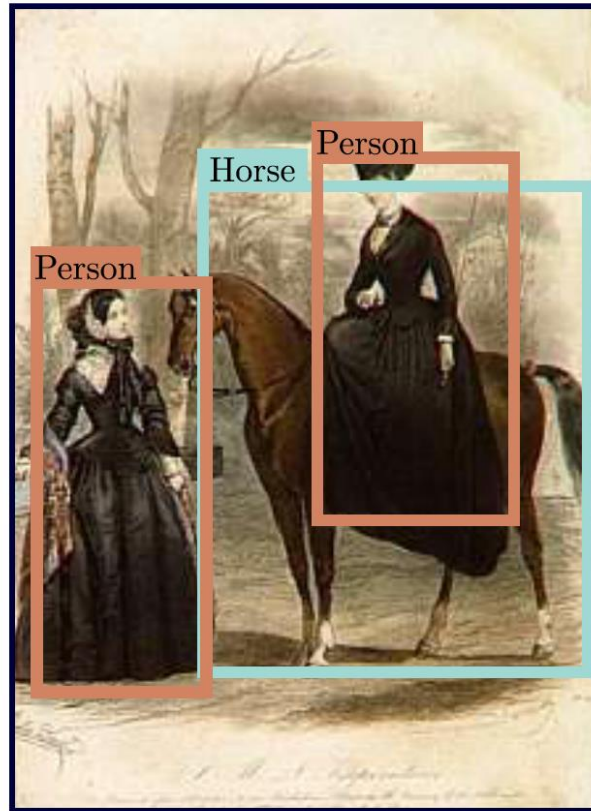
- Network similar to VGG (448x448 input)
- 7×7 grid of locations
- Predict class at each location
- Predict 2 bounding boxes at each location
 - Five parameters –x,y, height, width, and confidence
- Momentum, weight decay, dropout, and data augmentation
- Heuristic at the end to threshold and decide final boxes – (non maximum suppression)



Object detection (YOLO)



Results



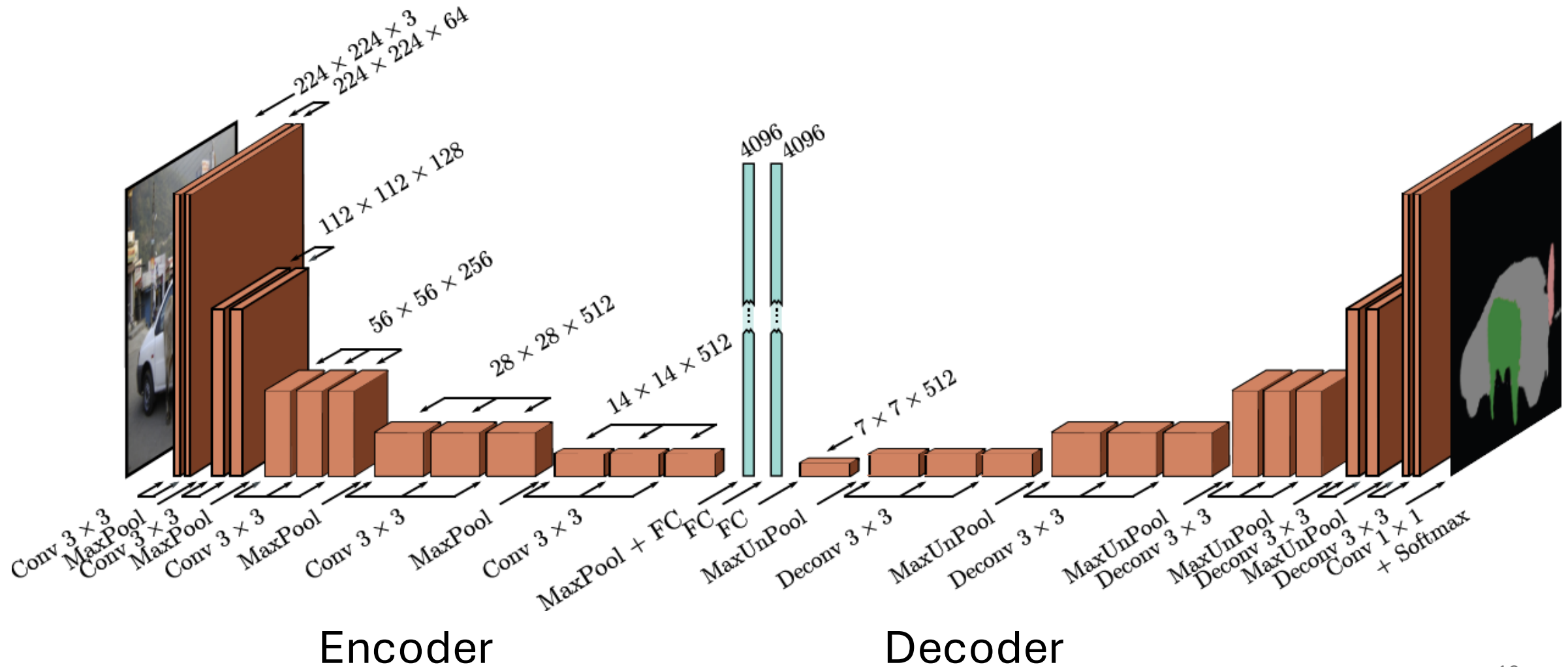
Any Questions?

???

Moving on

- Image classification
- Object detection
- Semantic segmentation

Semantic Segmentation (2015)

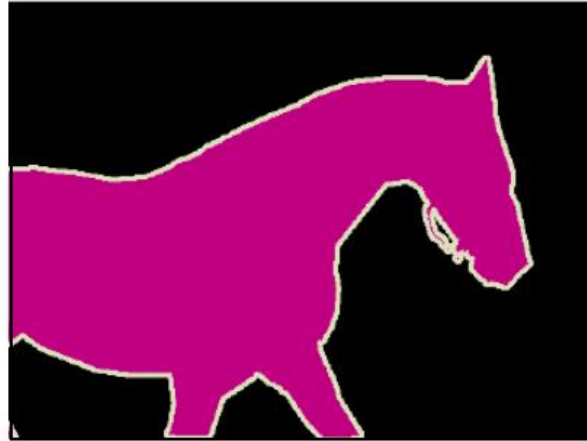


Semantic segmentation results

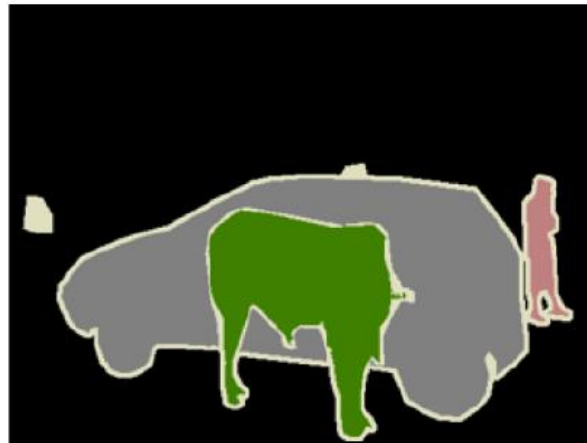
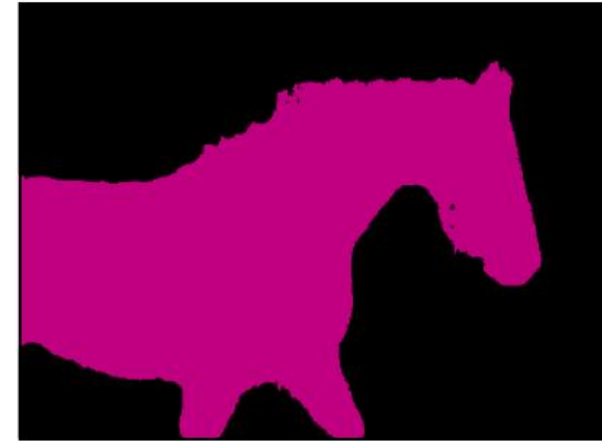
Input



Ground truth



Result



Any Questions?

- Finish up CNN examples (from last time)
 - Residual networks
- Challenges of deep networks
 - Residual connections and residual blocks
 - Exploding gradients in residual networks
 - Batch normalization
 - Common residual architectures

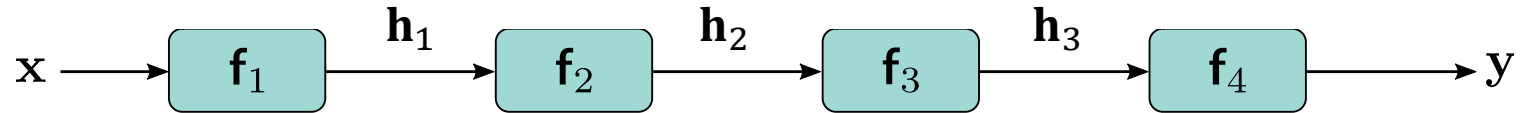
Previously we saw a sequential network:

$$\mathbf{h}_1 = \mathbf{f}_1[\mathbf{x}, \phi_1]$$

$$\mathbf{h}_2 = \mathbf{f}_2[\mathbf{h}_1, \phi_2]$$

$$\mathbf{h}_3 = \mathbf{f}_3[\mathbf{h}_2, \phi_3]$$

$$\mathbf{y} = \mathbf{f}_4[\mathbf{h}_3, \phi_4]$$



Fully connected network:

$$h_i = a \left[\beta_i + \sum_{j=1}^D \omega_{ij} x_j \right]$$

Convolutional network (e.g. 1 channel \rightarrow 1 channel):

$$\begin{aligned} h_i &= a \left[\beta + \omega_1 x_{i-1} + \omega_2 x_i + \omega_3 x_{i+1} \right] \\ &= a \left[\beta + \sum_{j=1}^3 \omega_j x_{i+j-2} \right] \end{aligned}$$

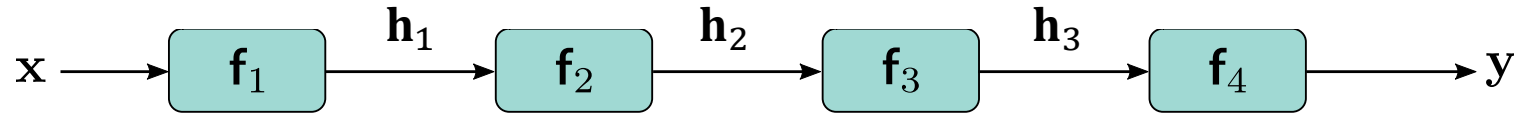
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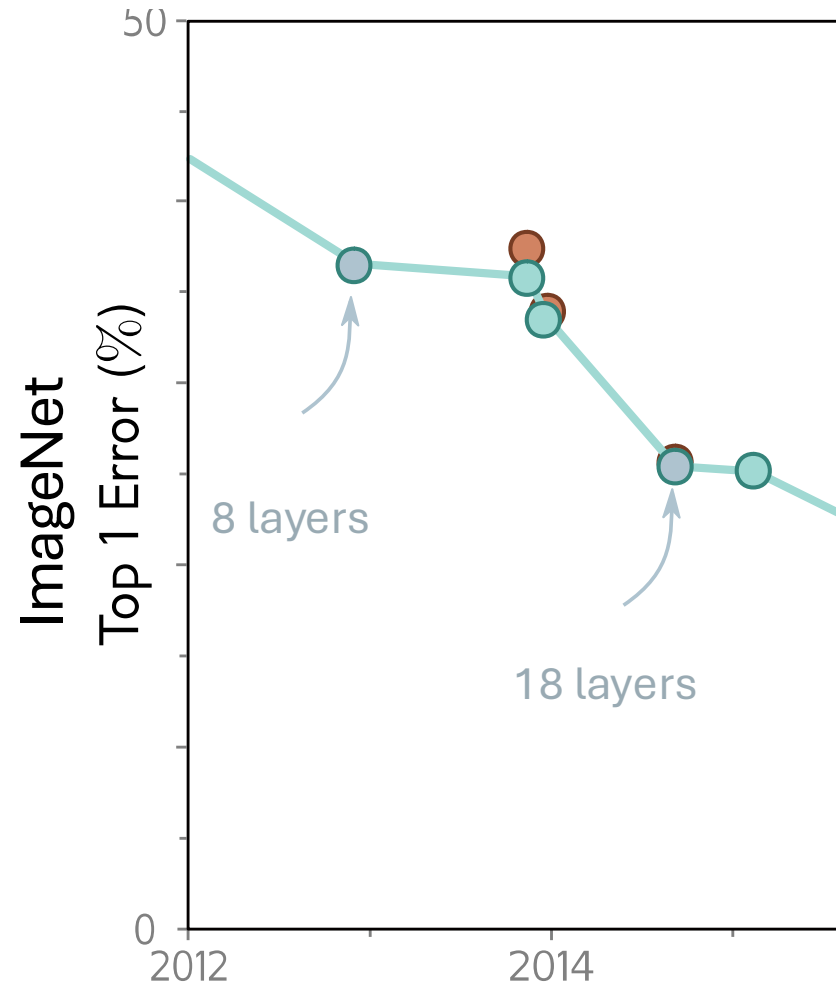
$$\mathbf{y} = \mathbf{f}_4[\mathbf{h}_3, \phi_4]$$



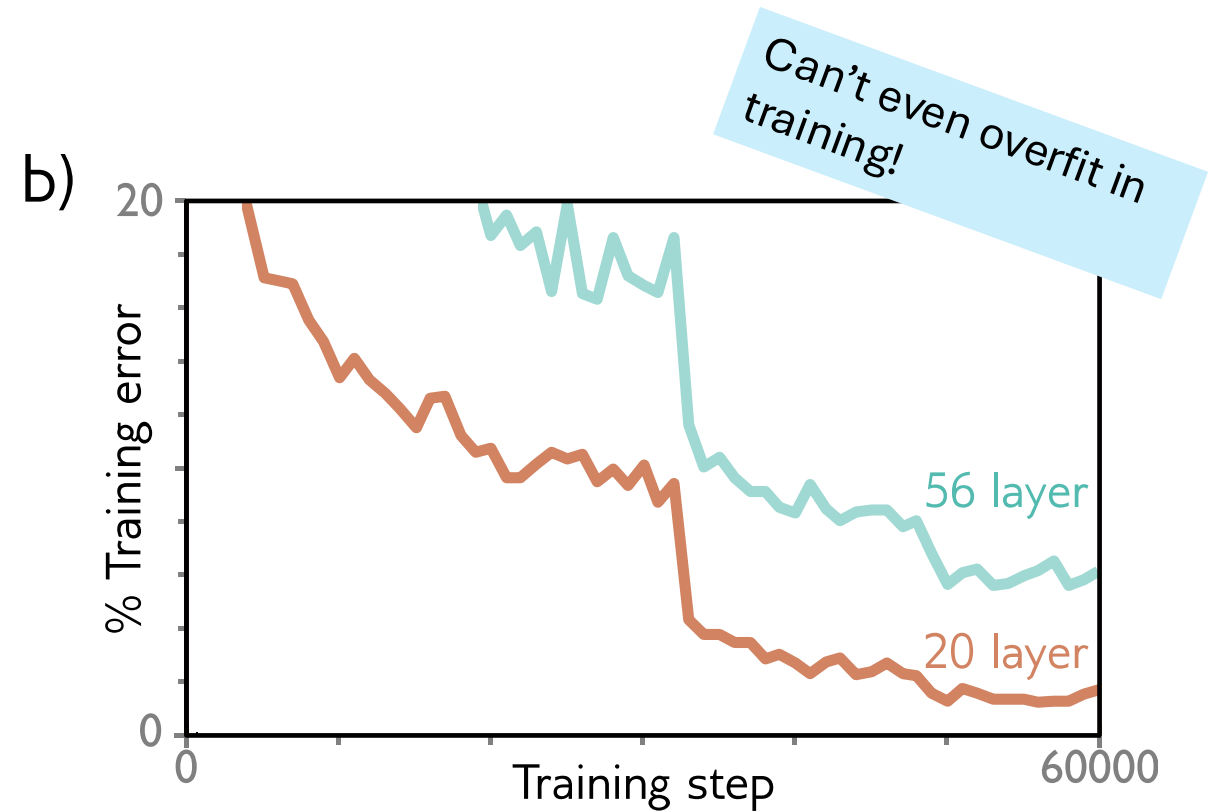
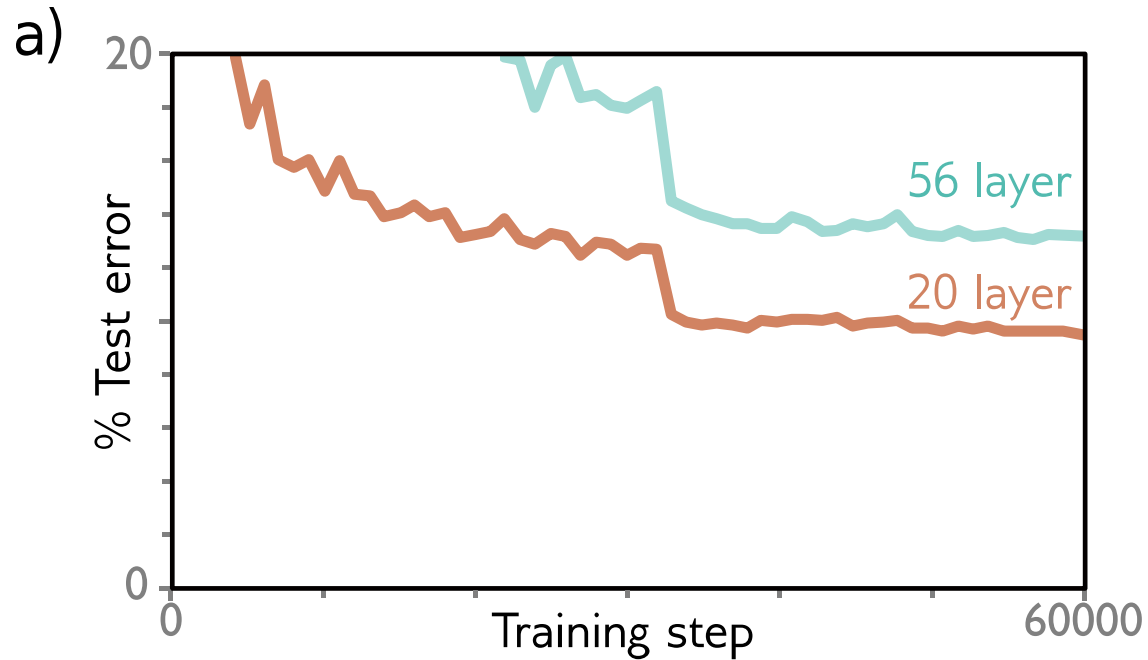
Can think of as a sequence of nested functions:

$$\mathbf{y} = \mathbf{f}_4 \left[\mathbf{f}_3 \left[\mathbf{f}_2 \left[\mathbf{f}_1[\mathbf{x}, \phi_1], \phi_2 \right], \phi_3 \right], \phi_4 \right]$$

More layers are better...



More layers are better... up to a point

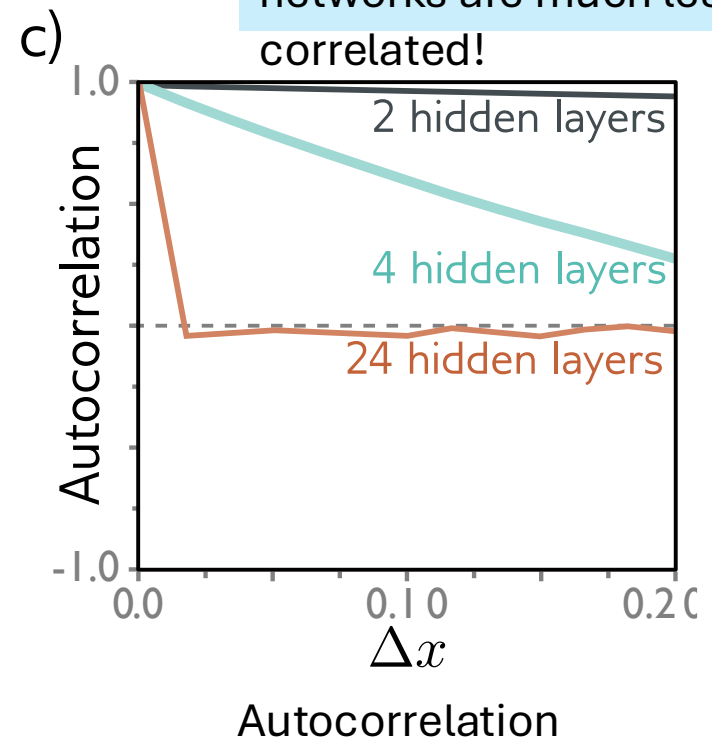
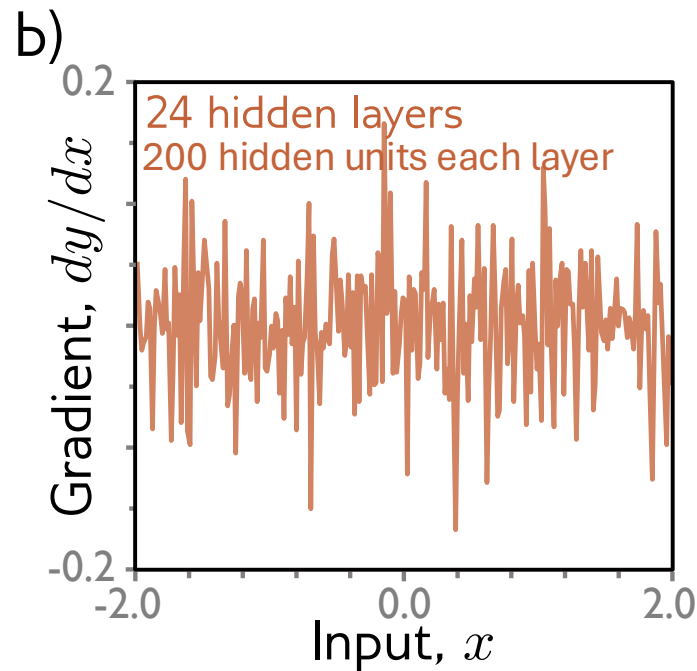
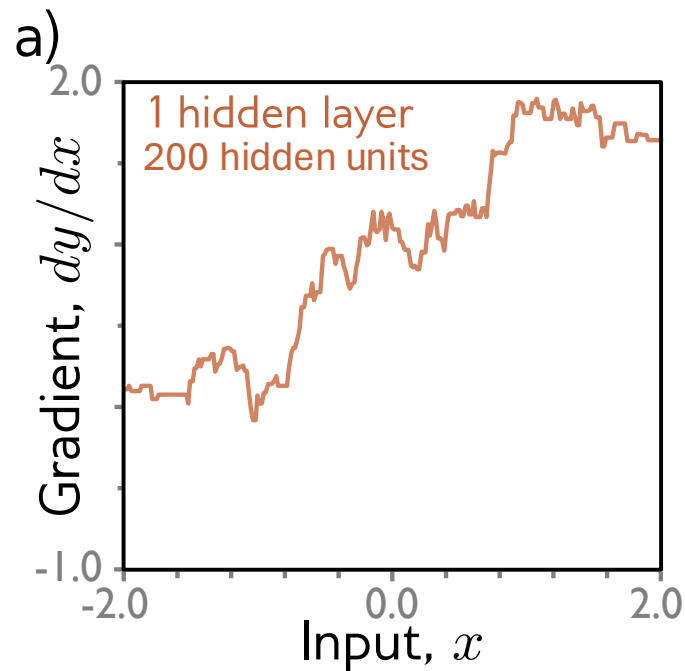


Convolutional Network on CIFAR10

What's going on?

Not completely understood, but...

Take a look at $\partial y / \partial x$ for shallow and deep networks.



Gradients of deeper networks are much less correlated!

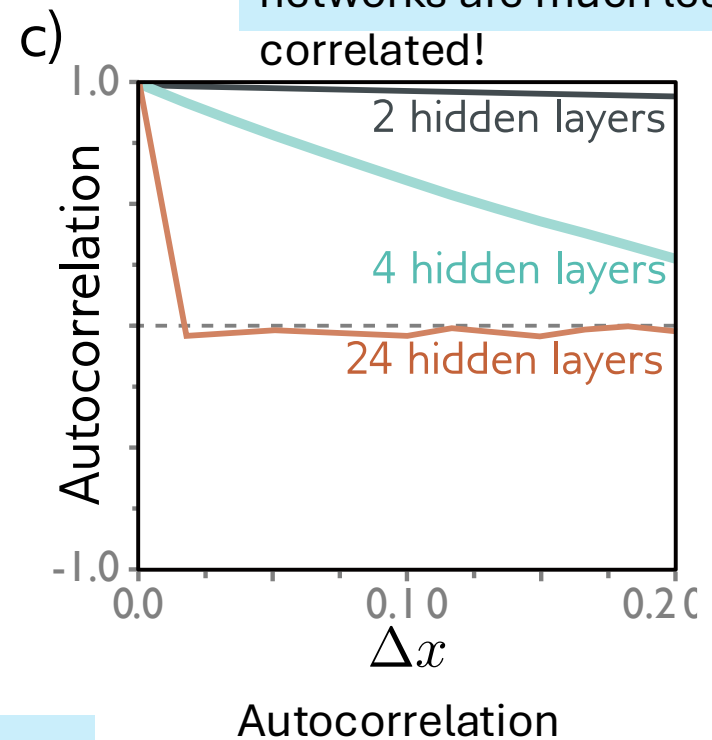
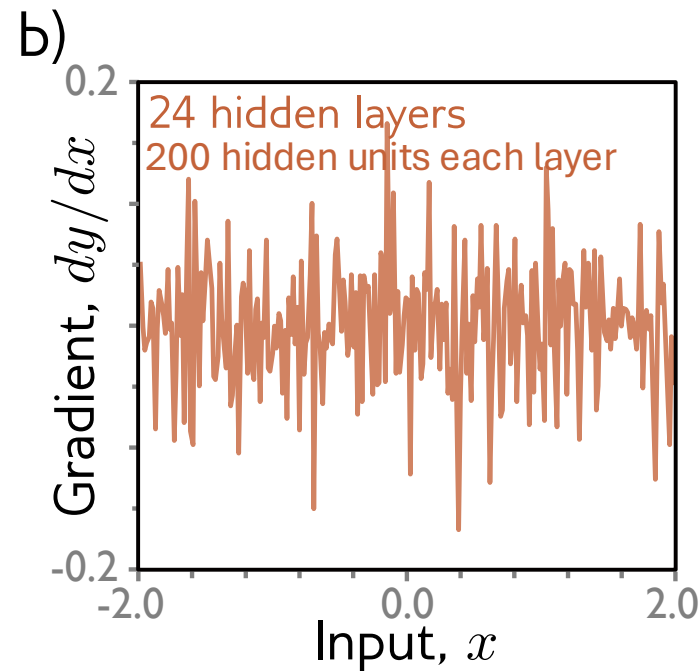
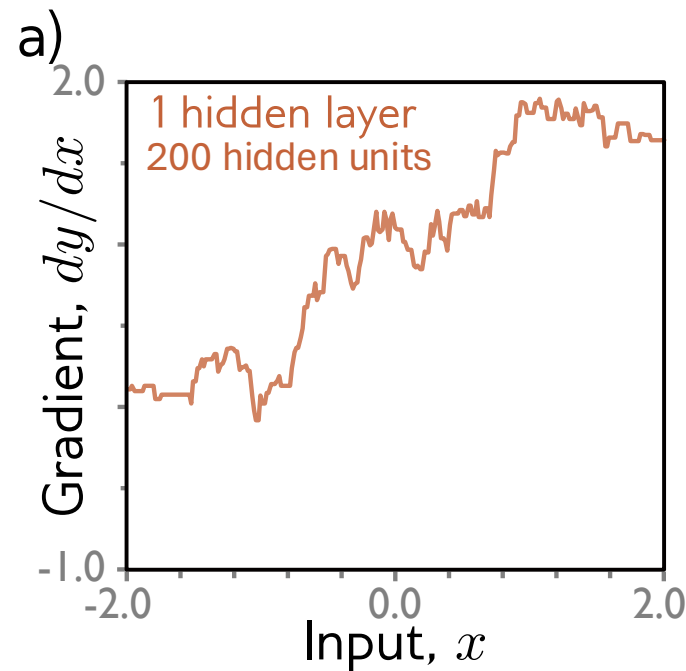
A small step in gradient descent may jump to wildly different valued gradient!

What's going on?

The Shattered Gradient Phenomenon

Not completely understood, but...

Take a look at $\partial y / \partial x$ for shallow and deep networks.

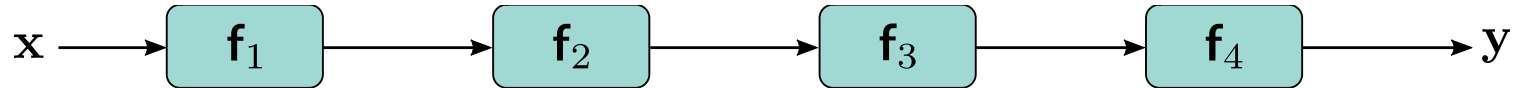


Gradients of deeper networks are much less correlated!

A small step in gradient descent may jump to wildly different valued gradient!

What's going on?

The Shattered Gradient Phenomenon



$$y = f_4 \left[f_3 \left[f_2 \left[f_1[x, \phi_1], \phi_2 \right], \phi_3 \right], \phi_4 \right]$$

The derivative of the output y w.r.t. the first layer f_1 is, by the chain rule:

$$\frac{\partial y}{\partial f_1} = \frac{\partial f_4}{\partial f_3} \frac{\partial f_3}{\partial f_2} \frac{\partial f_2}{\partial f_1}$$

f_1 impacts f_2 impacts f_3 , etc...

Any Questions?

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Solution: Residual connections

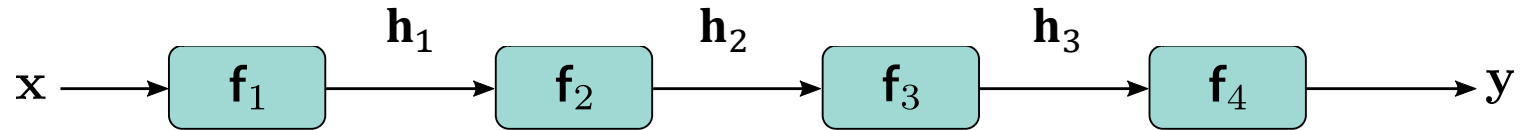
Regular sequential network:

$$\mathbf{h}_1 = \mathbf{f}_1[\mathbf{x}, \phi_1]$$

$$\mathbf{h}_2 = \mathbf{f}_2[\mathbf{h}_1, \phi_2]$$

$$\mathbf{h}_3 = \mathbf{f}_3[\mathbf{h}_2, \phi_3]$$

$$\mathbf{y} = \mathbf{f}_4[\mathbf{h}_3, \phi_4]$$



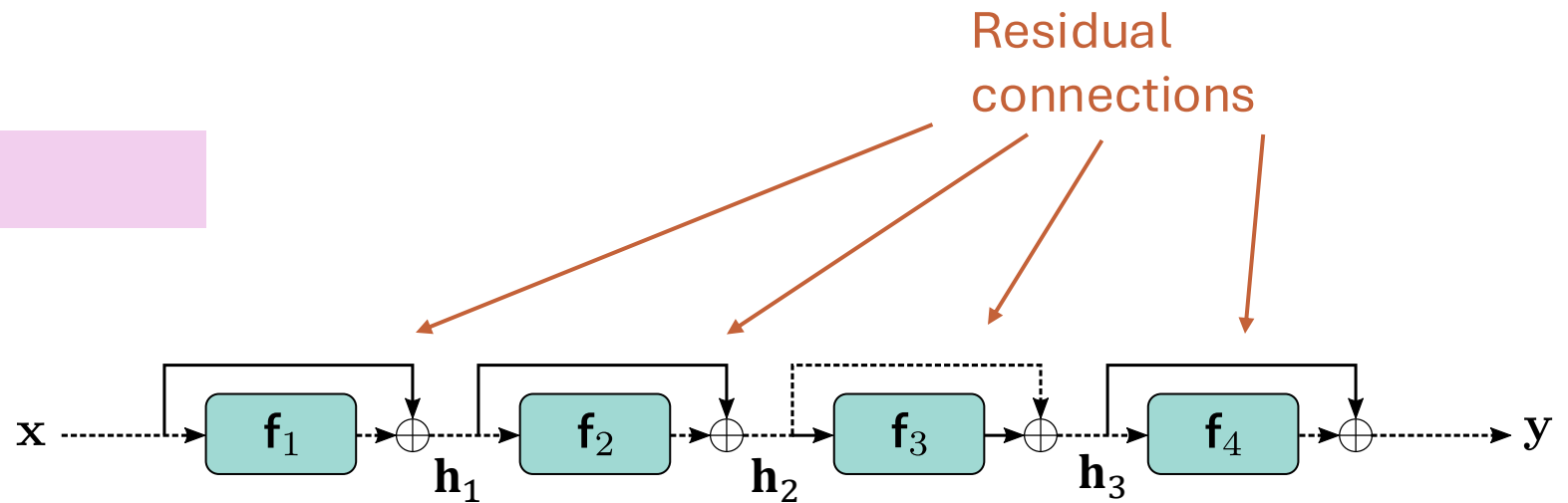
Residual network:

$$\mathbf{h}_1 = \mathbf{x} + \mathbf{f}_1[\mathbf{x}, \phi_1]$$

$$\mathbf{h}_2 = \mathbf{h}_1 + \mathbf{f}_2[\mathbf{h}_1, \phi_2]$$

$$\mathbf{h}_3 = \mathbf{h}_2 + \mathbf{f}_3[\mathbf{h}_2, \phi_3]$$

$$\mathbf{y} = \mathbf{h}_3 + \mathbf{f}_4[\mathbf{h}_3, \phi_4]$$



Residual Network

$$\mathbf{h}_1 = \mathbf{x} + \mathbf{f}_1[\mathbf{x}, \phi_1]$$

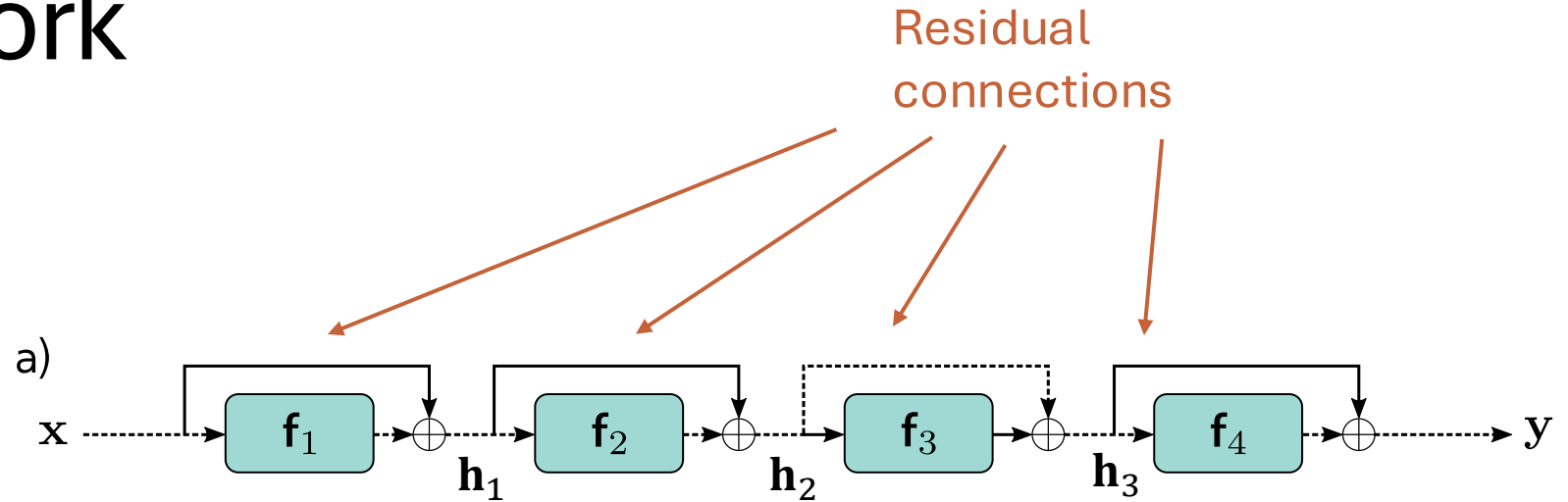
$$\mathbf{h}_2 = \mathbf{h}_1 + \mathbf{f}_2[\mathbf{h}_1, \phi_2]$$

$$\mathbf{h}_3 = \mathbf{h}_2 + \mathbf{f}_3[\mathbf{h}_2, \phi_3]$$

$$\mathbf{y} = \mathbf{h}_3 + \mathbf{f}_4[\mathbf{h}_3, \phi_4]$$

Substituting in:

$$\begin{aligned} \mathbf{y} = & \mathbf{x} + \mathbf{f}_1[\mathbf{x}] \\ & + \mathbf{f}_2[\mathbf{x} + \mathbf{f}_1[\mathbf{x}]] \\ & + \mathbf{f}_3[\mathbf{x} + \mathbf{f}_1[\mathbf{x}] + \mathbf{f}_2[\mathbf{x} + \mathbf{f}_1[\mathbf{x}]]] \\ & + \mathbf{f}_4[\mathbf{x} + \mathbf{f}_1[\mathbf{x}] + \mathbf{f}_2[\mathbf{x} + \mathbf{f}_1[\mathbf{x}]] + \mathbf{f}_3[\mathbf{x} + \mathbf{f}_1[\mathbf{x}] + \mathbf{f}_2[\mathbf{x} + \mathbf{f}_1[\mathbf{x}]]]] \end{aligned}$$



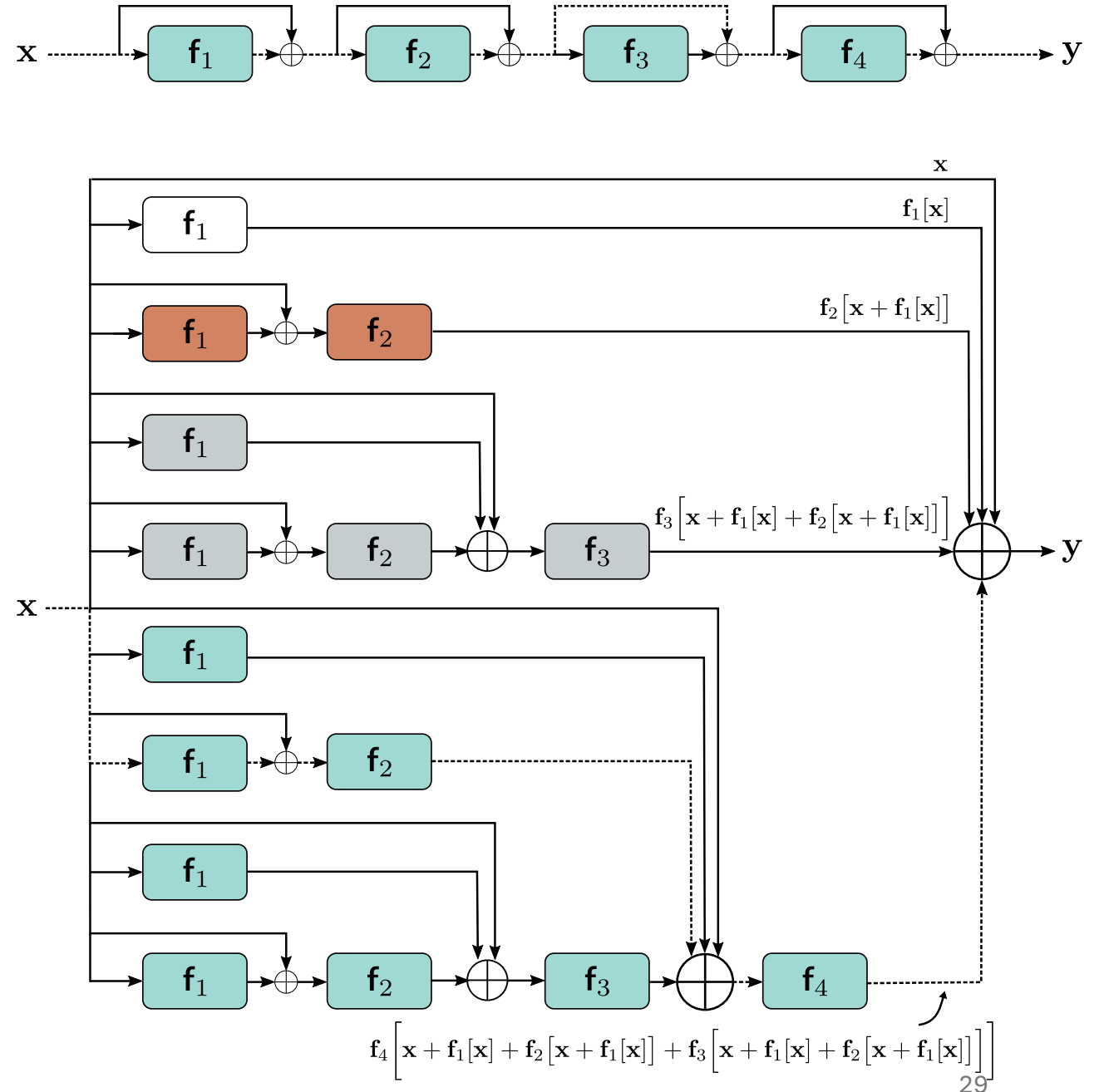
Think of optimizing f_1 , then f_2 , ...

Residual Network

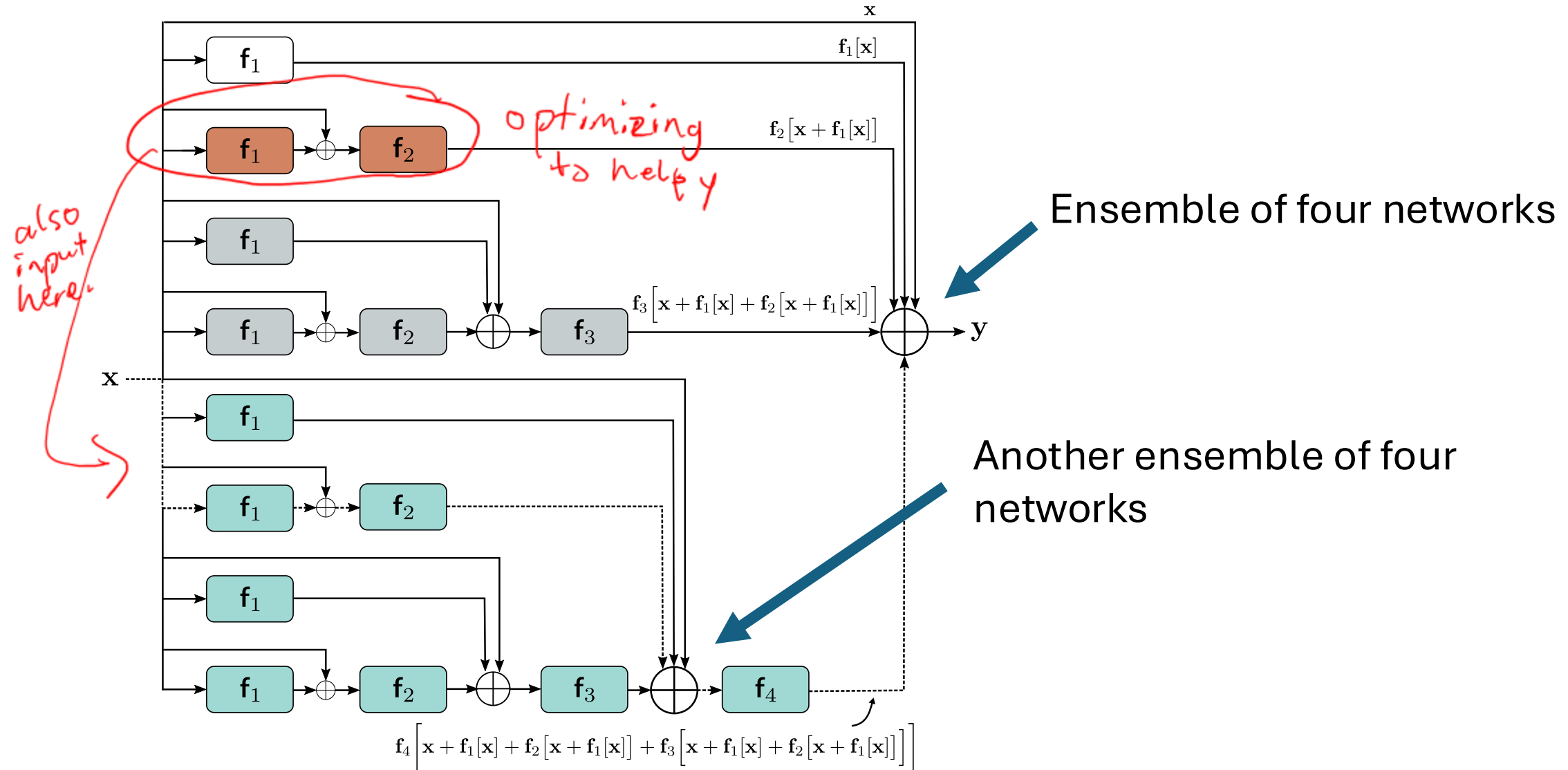
We can unravel all the possible paths

The output is the sum of the input plus 4 partial networks.

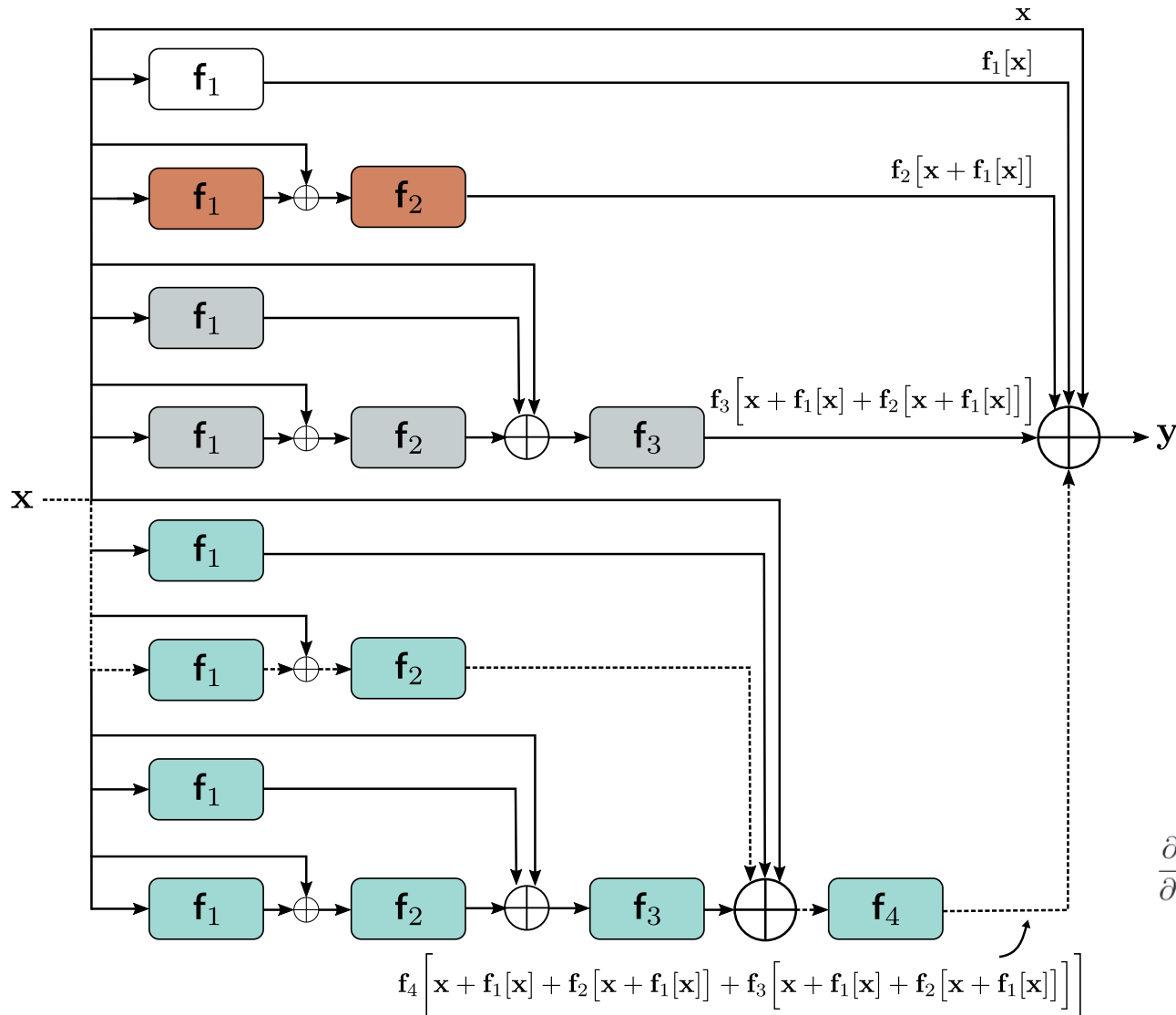
$$\begin{aligned}
 y = & x + f_1[x] \\
 & + f_2[x + f_1[x]] \\
 & + f_3[x + f_1[x] + f_2[x + f_1[x]]] \\
 & + f_4[x + f_1[x] + f_2[x + f_1[x]] + f_3[x + f_1[x] + f_2[x + f_1[x]]]]
 \end{aligned}$$



Residual Network as Ensemble of Networks



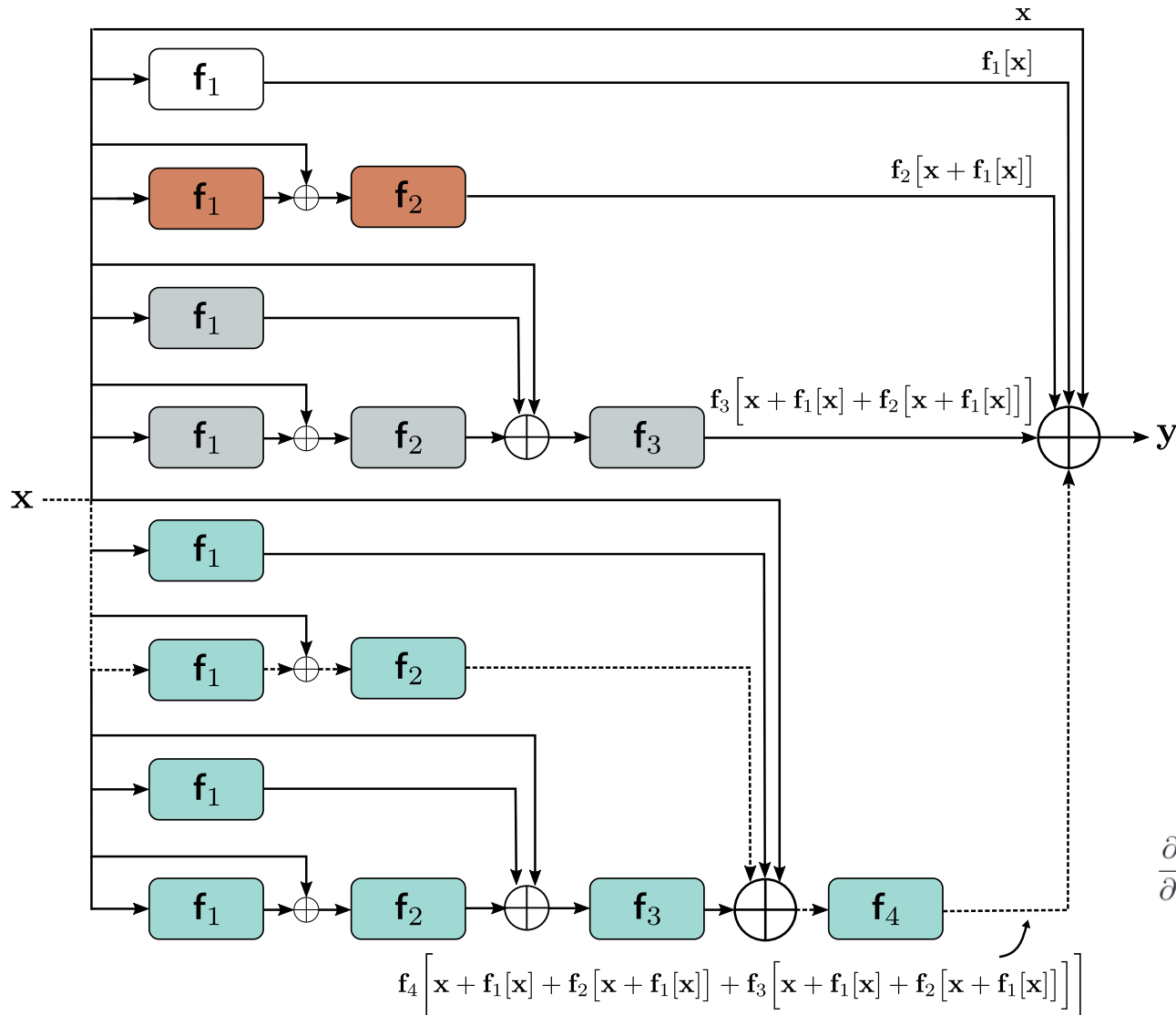
Residual Network as Ensemble of Networks



- 16 possible paths through the network!
- 8 paths include f_1
- The influence of f_1 on $\partial y / \partial f_1$ takes 8 different forms
- Gradients on shorter paths generally better behaved.

$$\frac{\partial y}{\partial f_1} = \mathbf{I} + \frac{\partial f_2}{\partial f_1} + \left(\frac{\partial f_3}{\partial f_1} + \frac{\partial f_3}{\partial f_2} \frac{\partial f_2}{\partial f_1} \right) + \left(\frac{\partial f_4}{\partial f_1} + \frac{\partial f_4}{\partial f_2} \frac{\partial f_2}{\partial f_1} + \frac{\partial f_4}{\partial f_3} \frac{\partial f_3}{\partial f_1} + \frac{\partial f_4}{\partial f_3} \frac{\partial f_3}{\partial f_2} \frac{\partial f_2}{\partial f_1} \right)$$

Residual Network as Ensemble of Networks

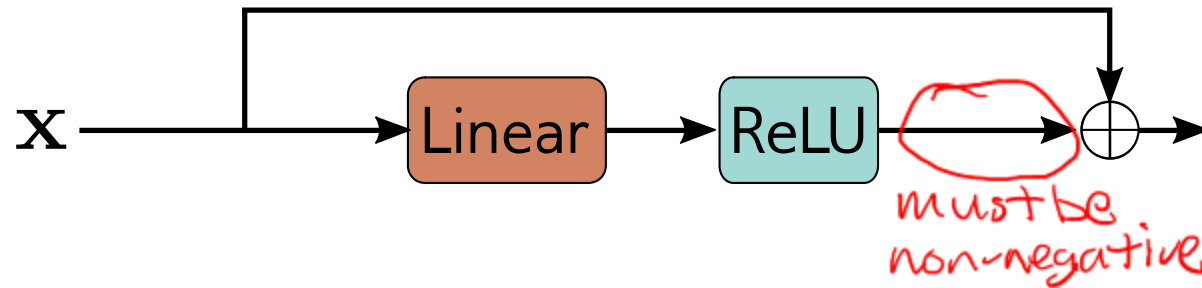


During training, the model can amplify or attenuate the different paths to achieve the best results

$$\frac{\partial y}{\partial f_1} = \mathbf{I} + \frac{\partial f_2}{\partial f_1} + \left(\frac{\partial f_3}{\partial f_1} + \frac{\partial f_3}{\partial f_2} \frac{\partial f_2}{\partial f_1} \right) + \left(\frac{\partial f_4}{\partial f_1} + \frac{\partial f_4}{\partial f_2} \frac{\partial f_2}{\partial f_1} + \frac{\partial f_4}{\partial f_3} \frac{\partial f_3}{\partial f_1} + \frac{\partial f_4}{\partial f_3} \frac{\partial f_3}{\partial f_2} \frac{\partial f_2}{\partial f_1} \right)$$

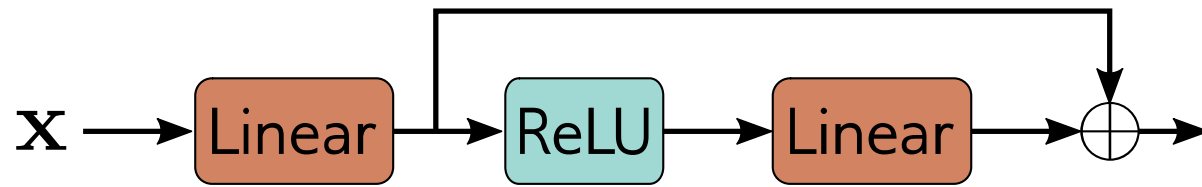
Order of operations is important

a) *Simple application of residual connection*



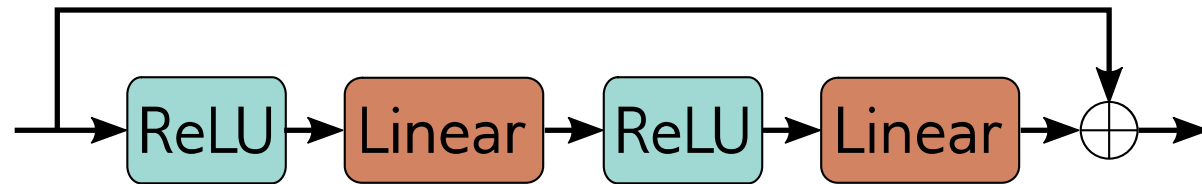
Can only add to the residual because of the ReLU

b)



More flexible approach to end with linear block.
Starting with linear block gives us some flexibility on spatial resolution.

c)



Note: if we start with a ReLU, then will clamp negative values and so do nothing

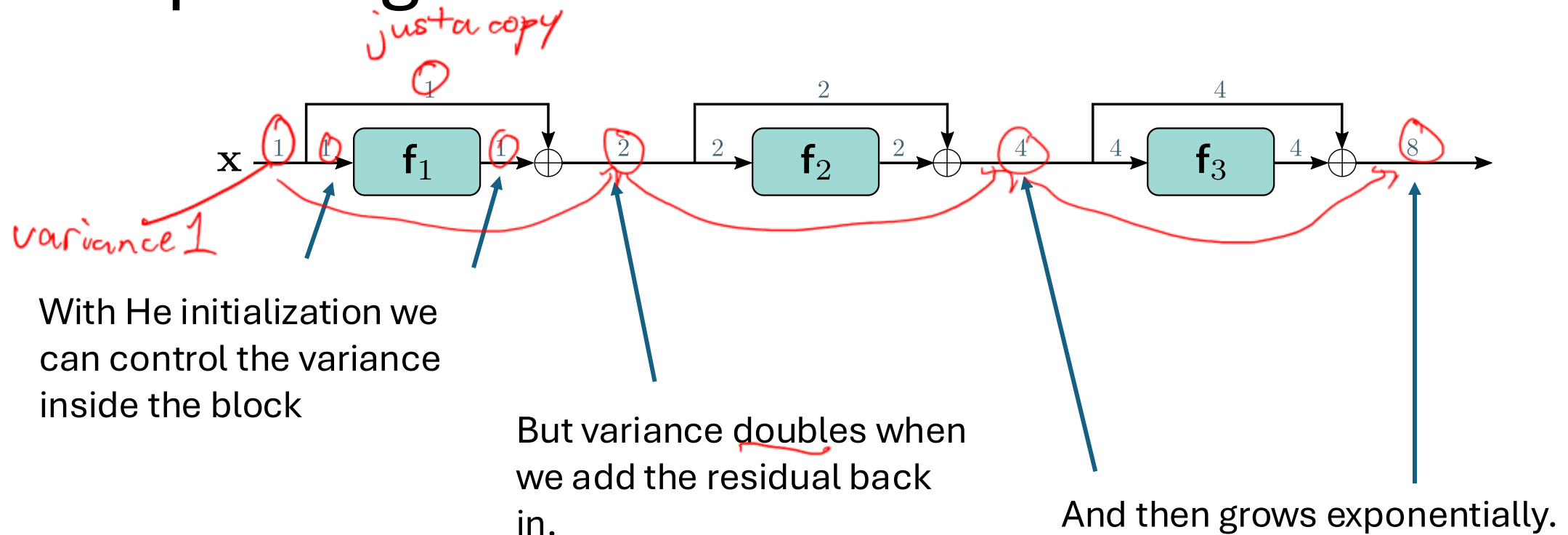
This helps increase depth
up to a point...

Any Questions?

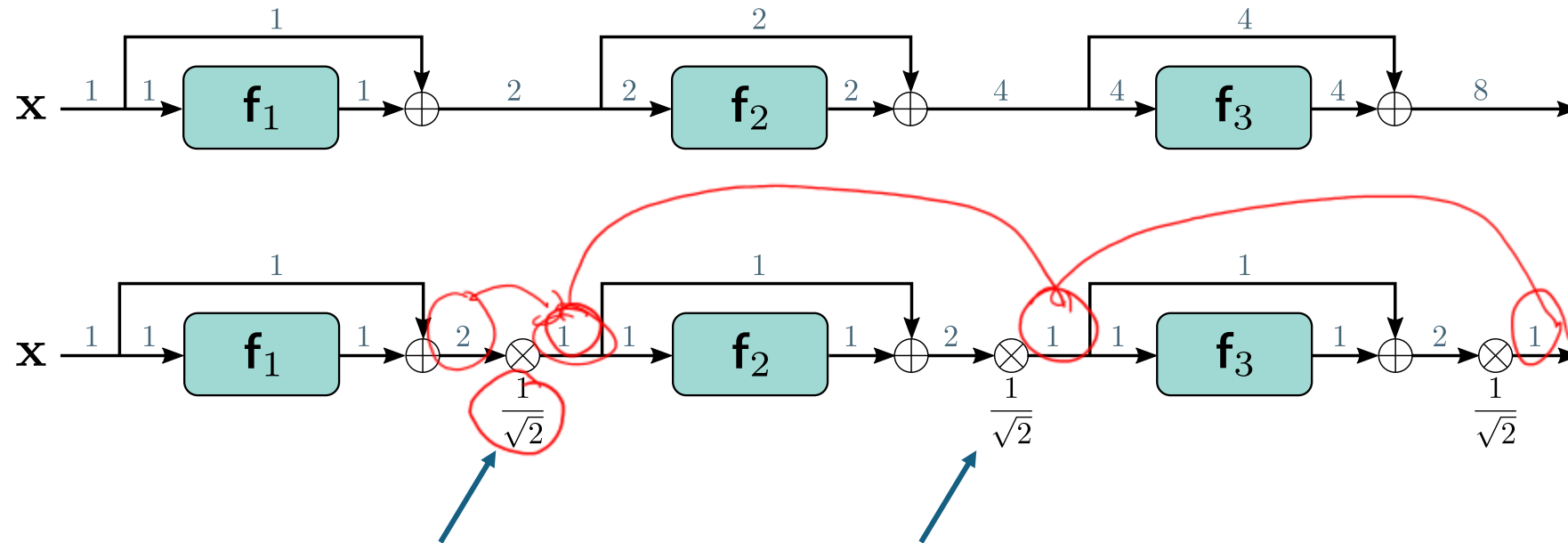


- Challenges of deep networks
- Residual connections and residual blocks
- Exploding gradients in residual networks
- Batch normalization
- Common residual architectures

Exploding Gradients in Residual Networks



Exploding Gradients in Residual Networks



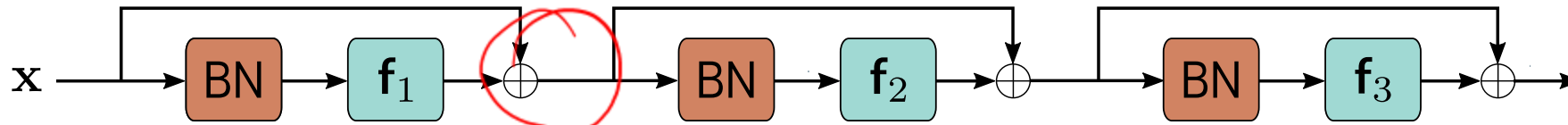
Could stabilize by renormalizing after adding each residual.

More common to apply *batch normalization*.

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Batch Normalization (a.k.a. *BatchNorm*)



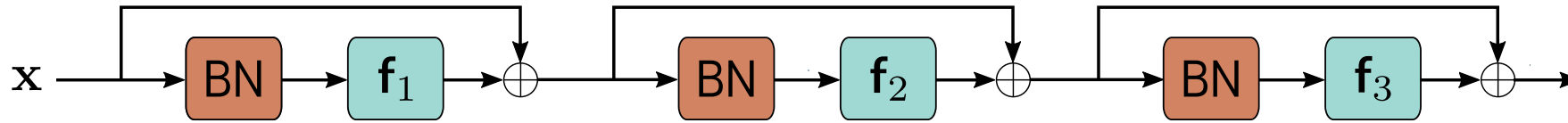
- Shifts and rescales each activation so that its mean and variance across the batch become values that are learned during training

fix the scaling w/o needing to assume correlation structure.

Collect stats from whole batch.

Use those to normalize batch to mean μ , std 1.

Batch Normalization (a.k.a. *BatchNorm*)

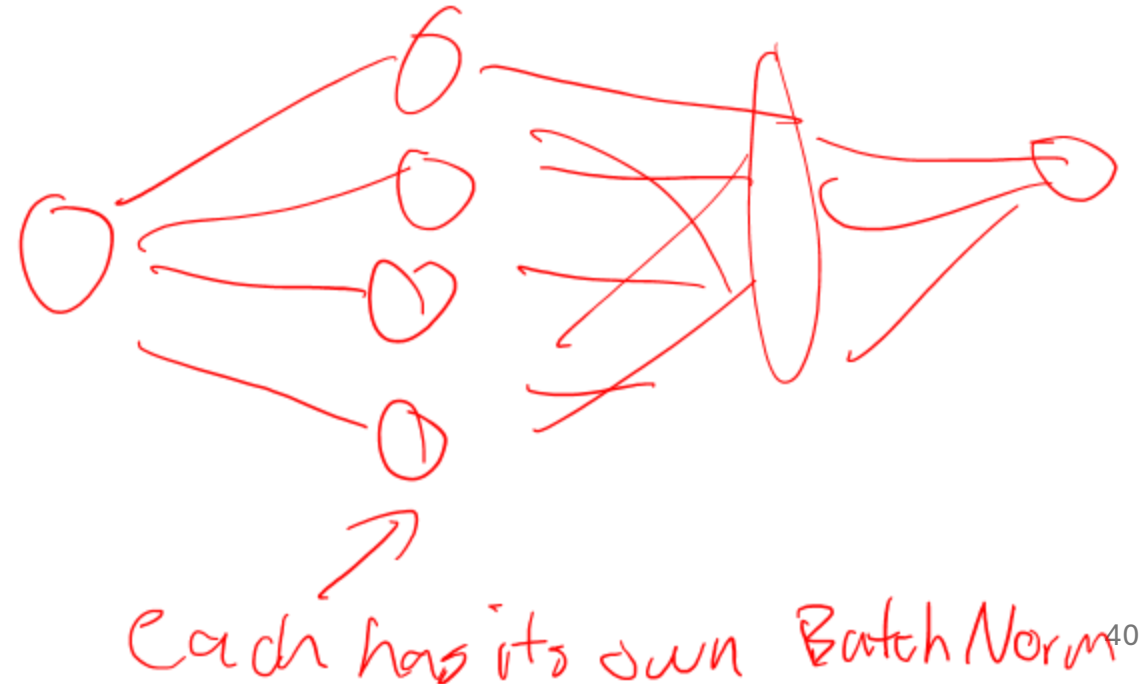


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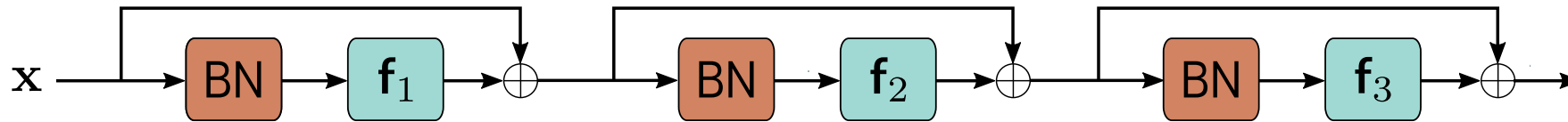
Calculate the sample *mean* and *standard deviation* for each hidden unit across samples of the batch.

$$m_h = \frac{1}{|\mathcal{B}|} \sum_{i \in \mathcal{B}} h_i$$

$$s_h = \sqrt{\frac{1}{|\mathcal{B}|} \sum_{i \in \mathcal{B}} (h_i - m_h)^2}$$



Batch Normalization (a.k.a. *BatchNorm*)



- Shifts and rescales each activation so that its mean and variance across the batch become values that are learned during training

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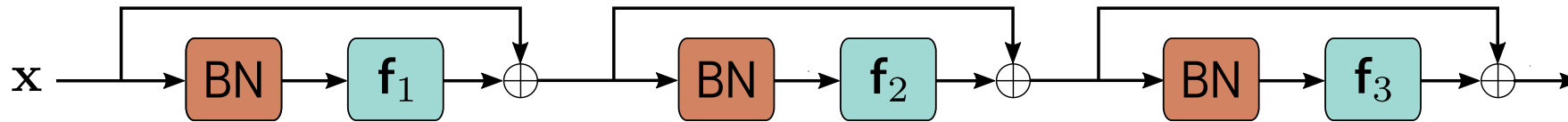
Standardize (normalize) to zero-mean and unit standard deviation.

$$\hat{h}_i \leftarrow \frac{h_i - m_h}{s_h + \epsilon} \quad \forall i \in \mathcal{B},$$

Scale by γ and shift by δ , which are *learned* parameters.

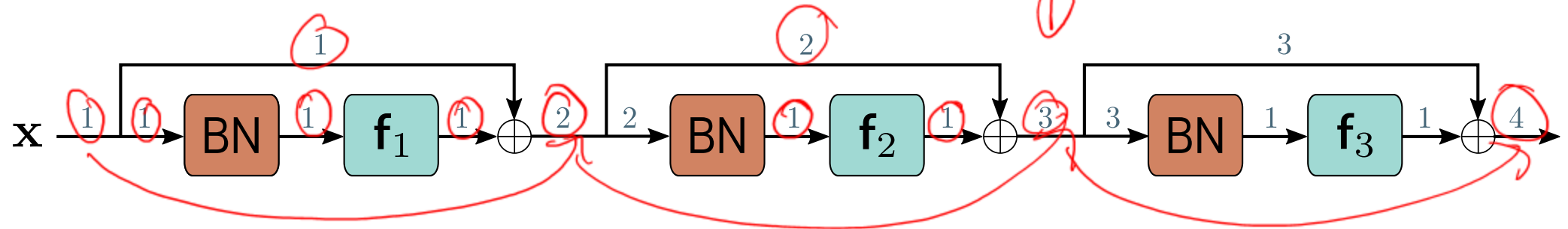
$$h_i \leftarrow \gamma \hat{h}_i + \delta \quad \forall i \in \mathcal{B}.$$

Batch Normalization (a.k.a. *BatchNorm*)



- Applied independently to each hidden unit
- **Standard FC Network** with K layers, each with D hidden units:
 KD learned scales, γ , and KD learned offset, δ
- **Convolutional Network** with K layers, each with C channels:
 KC learned scales, γ , and KC learned offset, δ

Benefits of BatchNorm



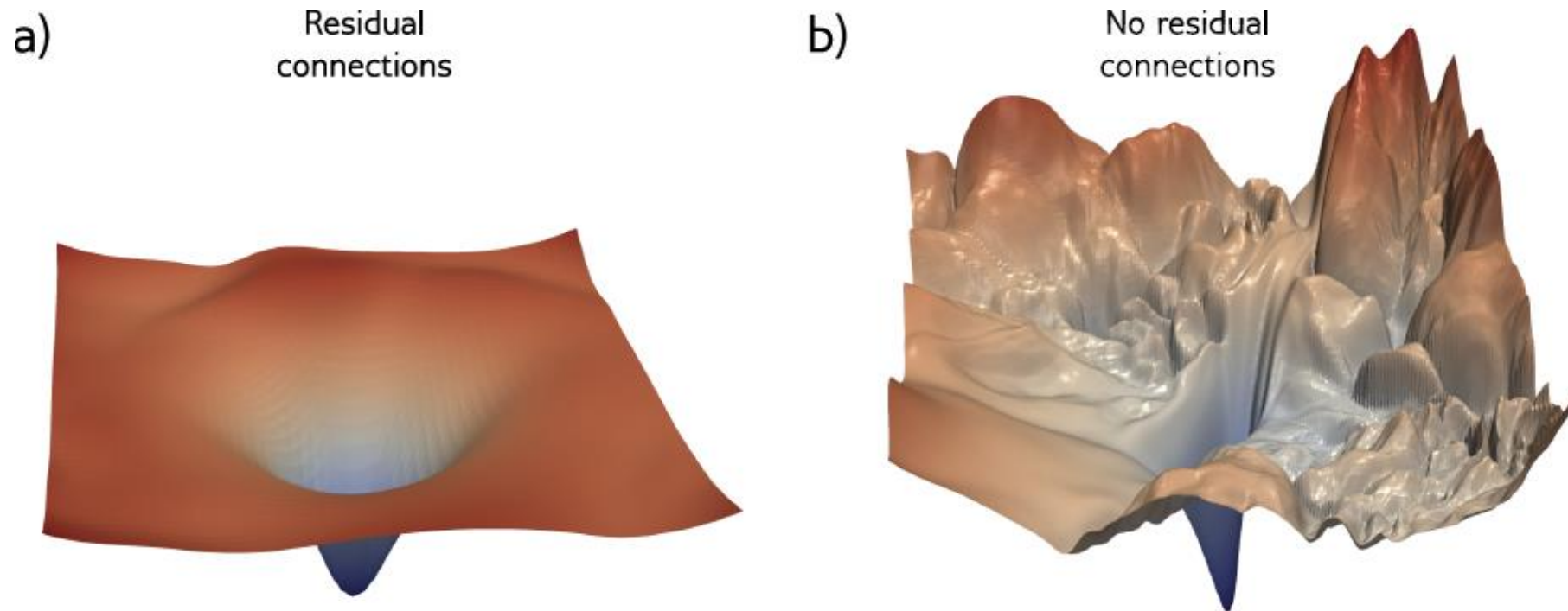
Stable forward propagation

- Initialize offsets δ to zero and scales γ to 1
- Variance now increases linearly
- k^{th} block adds *one unit of variance* to variance of k
- At initialization, later layers make smaller relative change to overall variation
- During training, the scales can increase in later layers if helpful
→ control the effective depth

Benefits of BatchNorm

Supports higher learning rates

Makes the loss surface smoother (reduces shattered gradients)



Benefits of BatchNorm

Regularization via added noise

BatchNorm injects noise since BN scale and shift depend on batch statistics.

Disadvantages of Batch Normalization

- Batch normalization makes results dependent on what else is in the same batch.
 - Much more likely if you group on target value.
- Layer normalization instead?
 - Similar spirit.
 - Normalize hidden layer activations of same input.
- Both actively used nowadays.



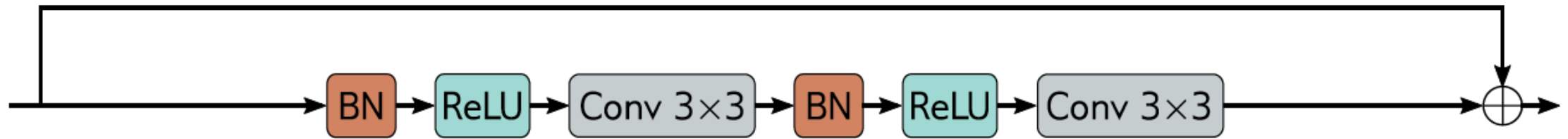
Any questions?



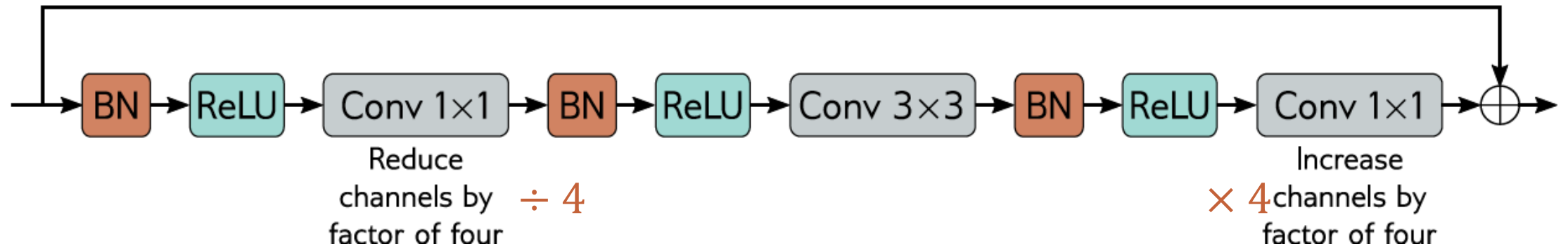
- Challenges of deep networks
- Residual connections and residual blocks
- Exploding gradients in residual networks
- Batch normalization
- Common residual architectures

ResNet (2015)

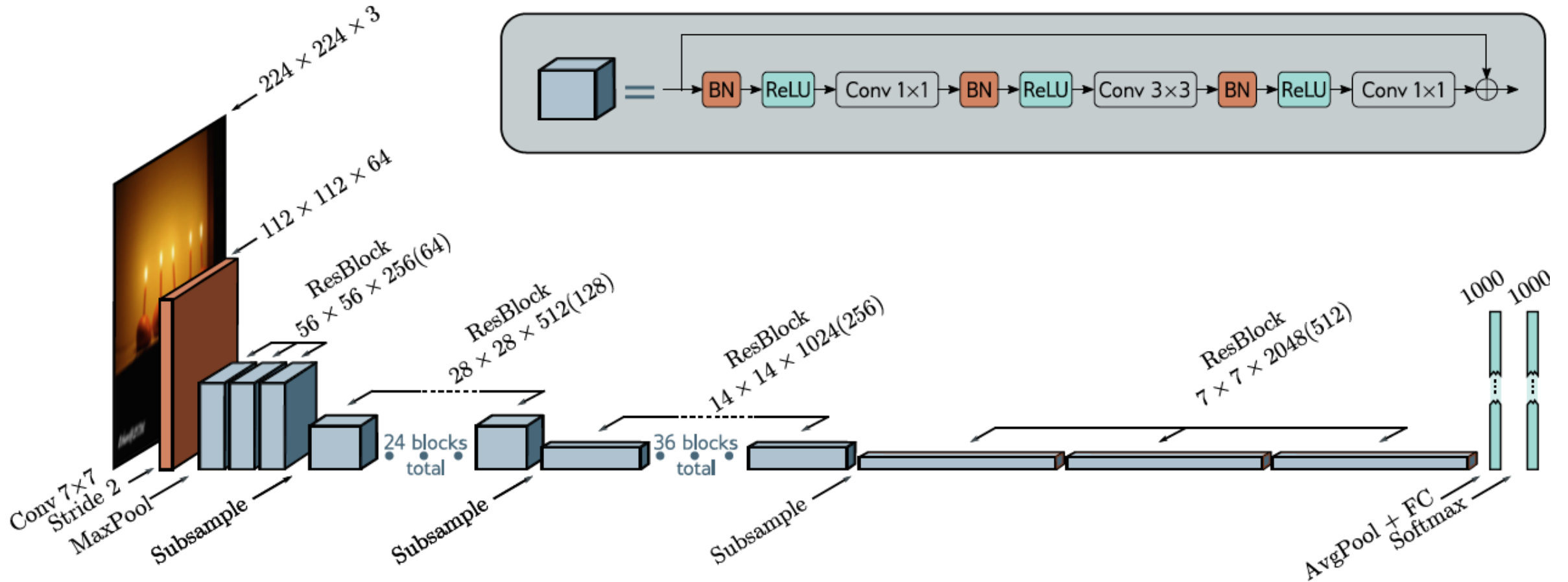
ResNet Block



Bottleneck Residual

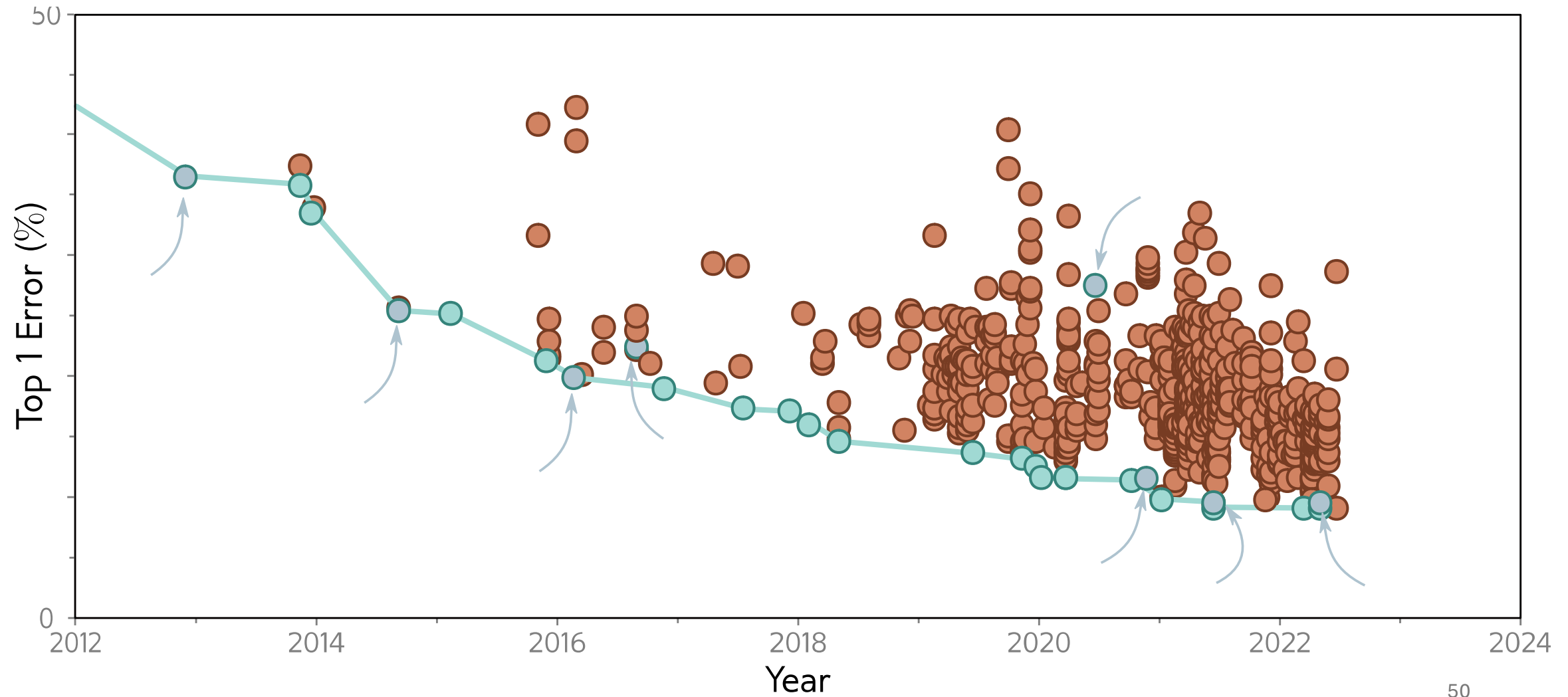


Resnet 200 (2016) for ImageNet Classification



K. He, X. Zhang, S. Ren, and J. Sun, "Deep Residual Learning for Image Recognition," *arXiv:1512.03385 [cs]*, Dec. 2015, <http://arxiv.org/abs/1512.03385>

ImageNet History



DenseNet

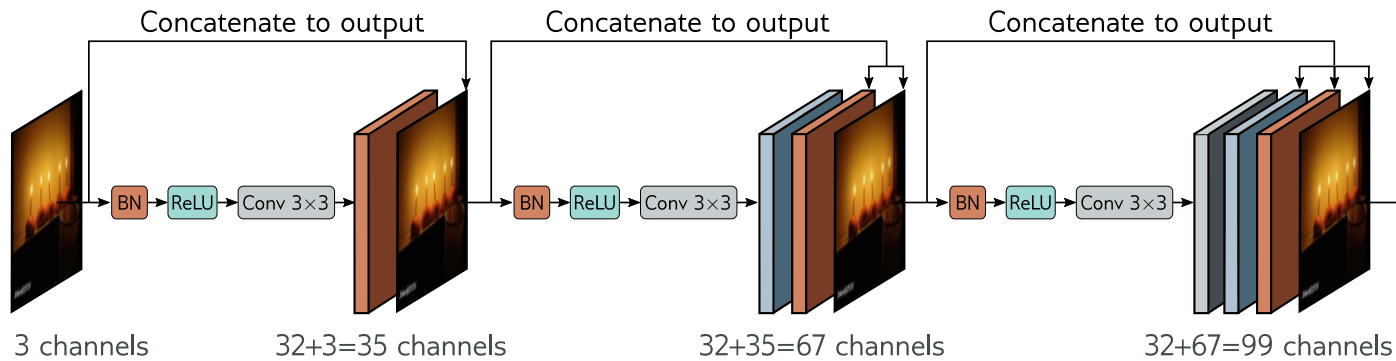


Figure from UDL

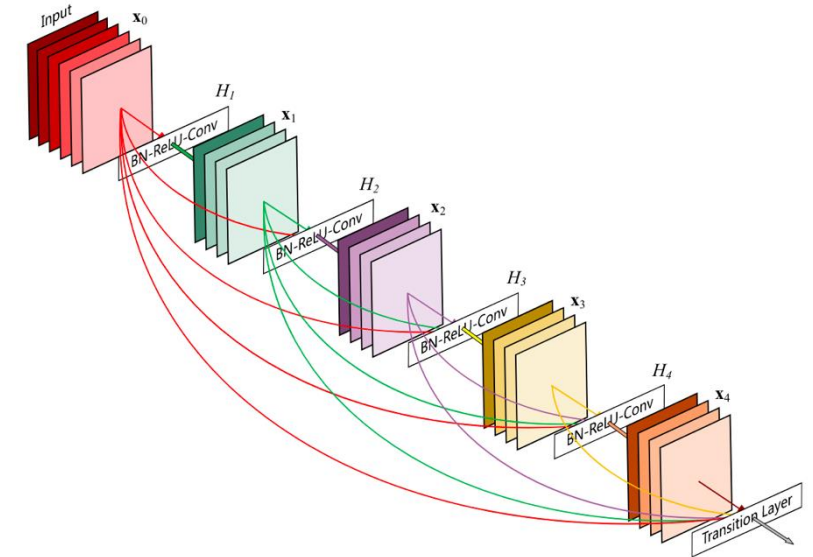
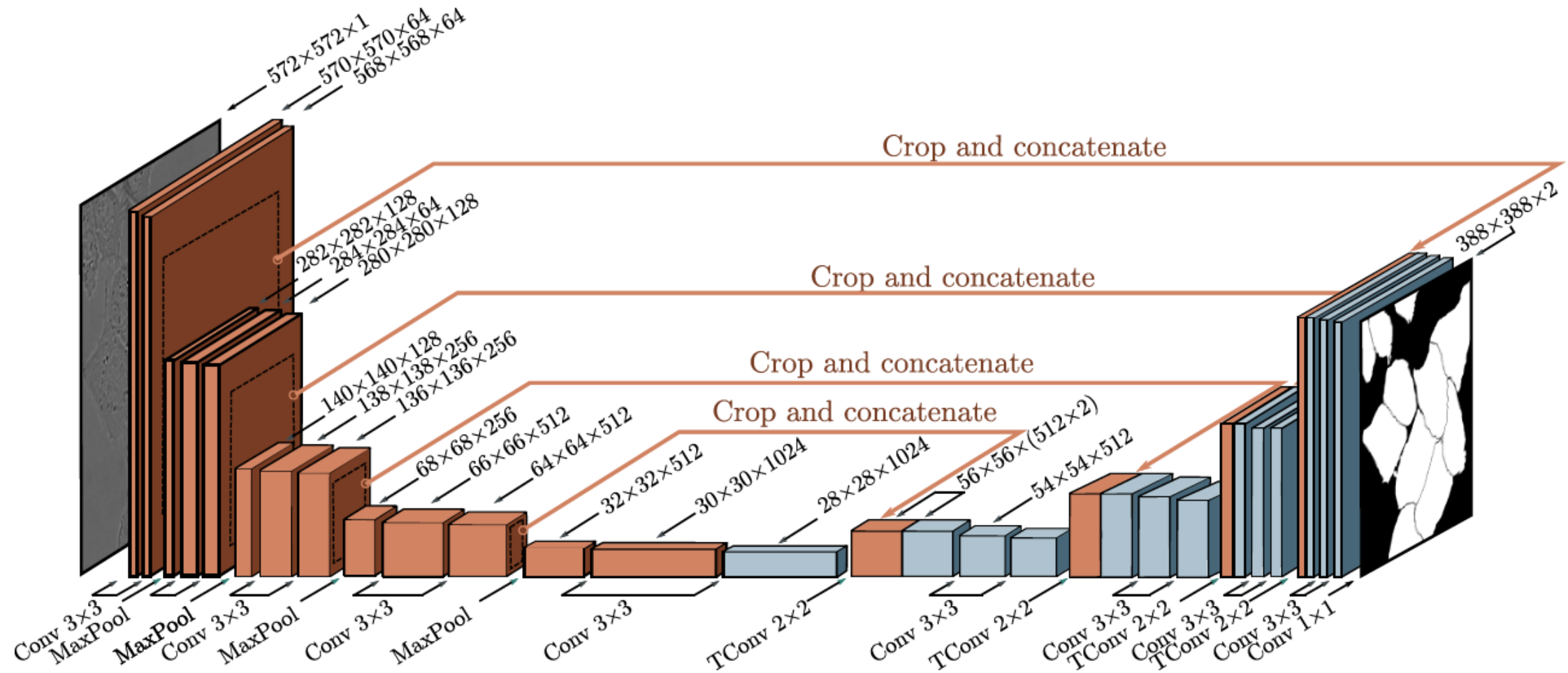


Figure 1: A 5-layer dense block with a growth rate of $k = 4$. Each layer takes all preceding feature-maps as input.

Figure from paper

U-Net (2016)



U-Net Results

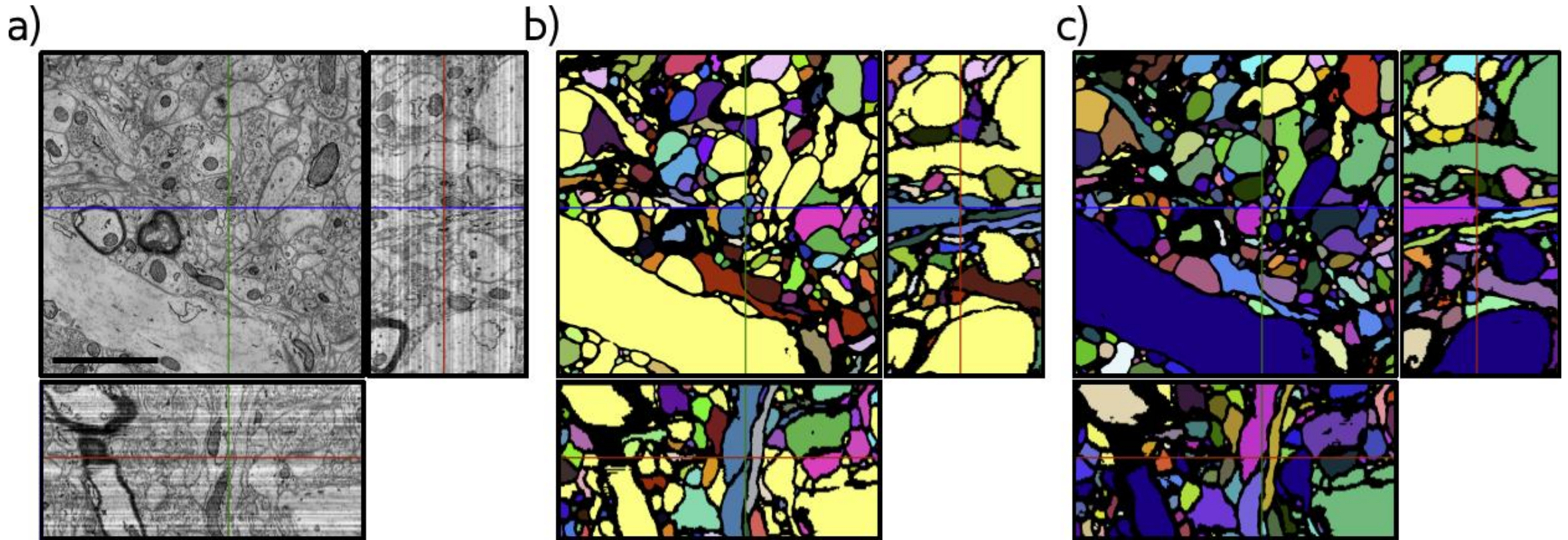
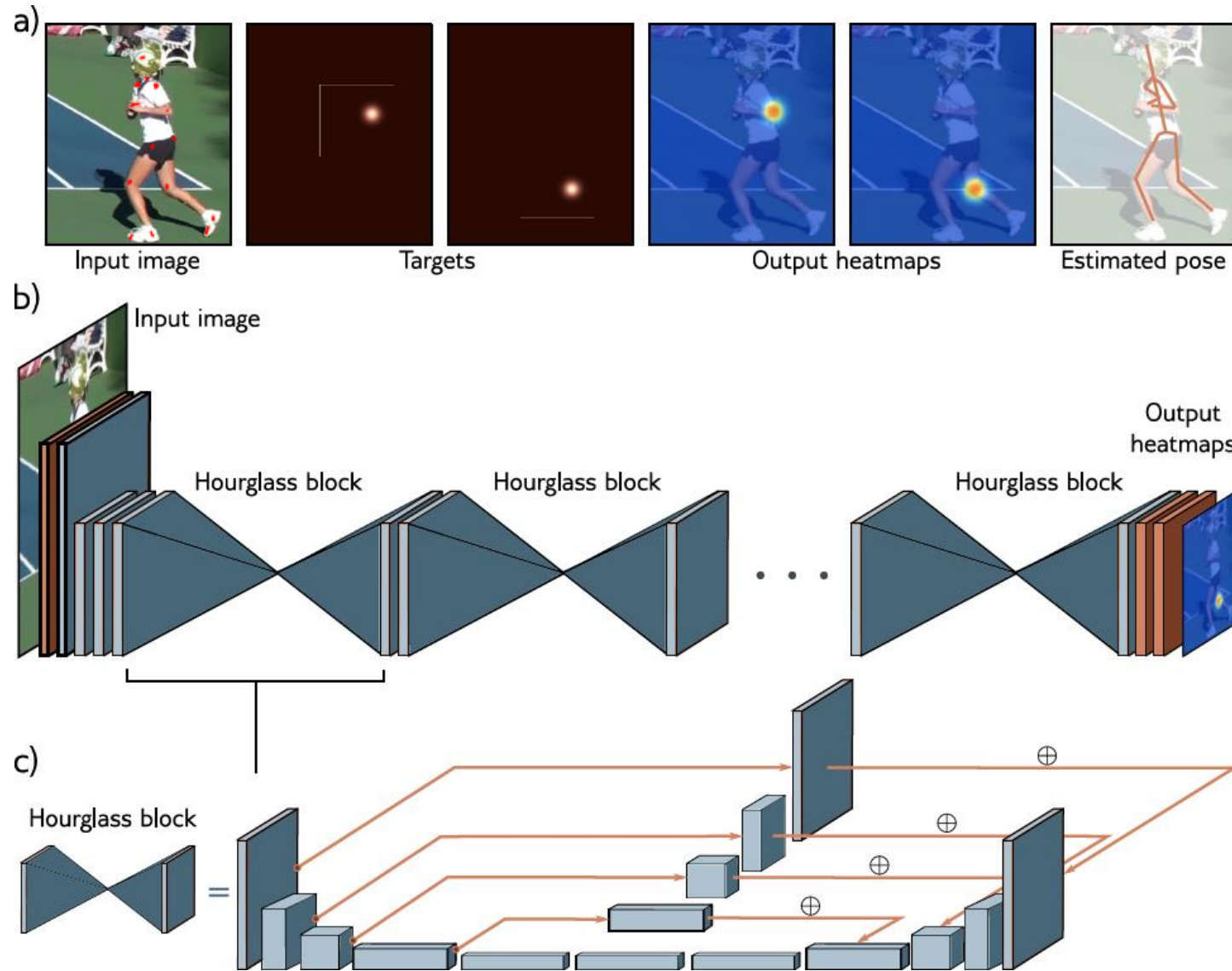


Figure 11.11 Segmentation using U-Net in 3D. a) Three slices through a 3D volume of mouse cortex taken by scanning electron microscope. b) A single U-Net is used to classify voxels as being inside or outside neurites. Connected regions are identified with different colors. c) For a better result, an ensemble of five U-Nets is trained, and a voxel is only classified as belonging to the cell if all five networks agree. Adapted from Falk et al. (2019).

Stacked hourglass networks for Pose Estimation



Any Questions?



- Challenges of deep networks
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